



# Introduction to SAMs and CGE Modeling

Using IFPRI's Dynamic CGE and Microsimulation Models

## Overview

- 1. Why Do Economywide Analysis?
- 2. Social Accounting Matrices (SAMs)
- 3. SAM Multiplier Analysis
- 4. Simple CGE Model
- 5. IFPRI Standard CGE Model
- 6. Microsoft-Excel<sup>®</sup> Interface
- 7. Extending the Standard Model

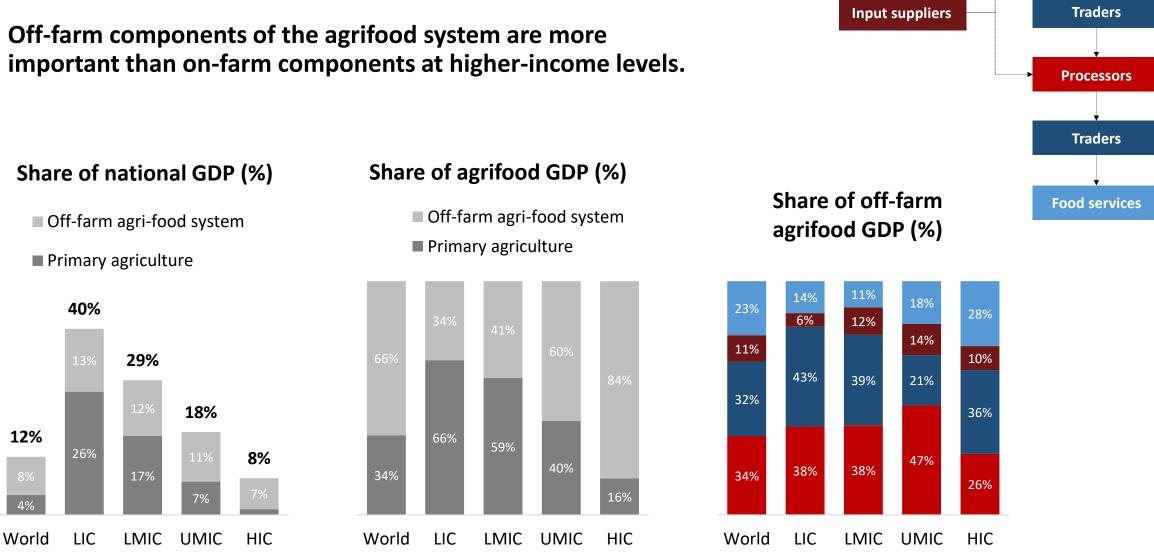


# Part 1

Why Do Economywide Analysis?

# **Agrifood Systems**

Off-farm components of the agrifood system are more important than on-farm components at higher-income levels.



**Agriculture** 

## **Private Sector**

#### **Public-Sector-Driven Transformation**

Actions government must undertake in most circumstances (e.g., infrastructure, education, R&D, extension services, etc.)

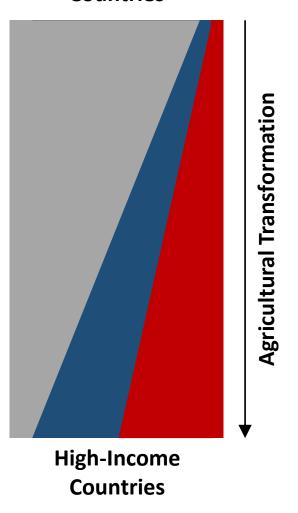
#### **Public-Private Sector Coordination**

Actions private sector will undertake if governments create an enabling environment (i.e., conducive policies & investments)

#### **Private-Sector-Driven Transformation**

Actions private sector will undertake on its own (e.g., supplying profitable input & output markets where demand is strong)

#### Low-Income Countries



## **Economywide Models**

## Computable General Equilibrium

### Economic linkages

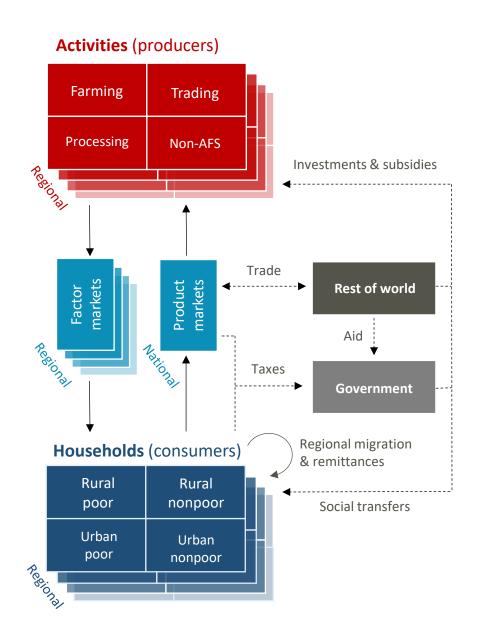
Between sectors, households, government & rest of world

## Resource competition

- Factor markets (land, labor, capital)
- Product markets (supply, demand)

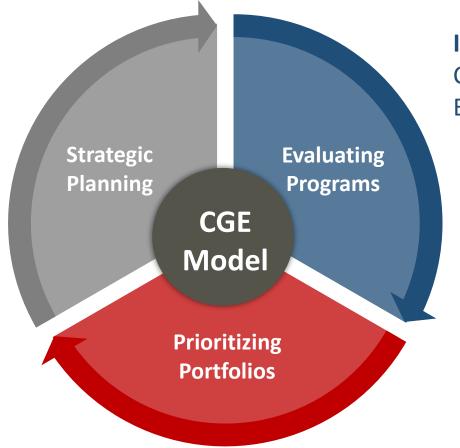
## Macro consistency

- Government (revenues, spending)
- Savings-investment
- Current account (foreign exchange)



## Types of Economywide Studies

Foresight Analysis
Tracking progress
Setting targets & goals

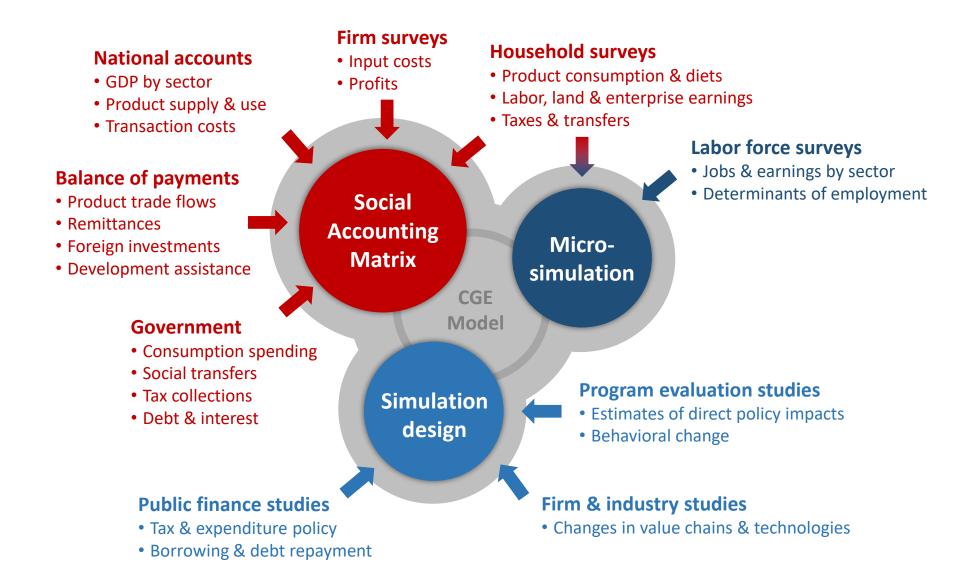


**Impact Evaluation** 

Capturing spillovers
Estimating benefits & costs

**Policy & Investment Choices**Identifying priorities, Optimizing budgets

## Data Reconciliation



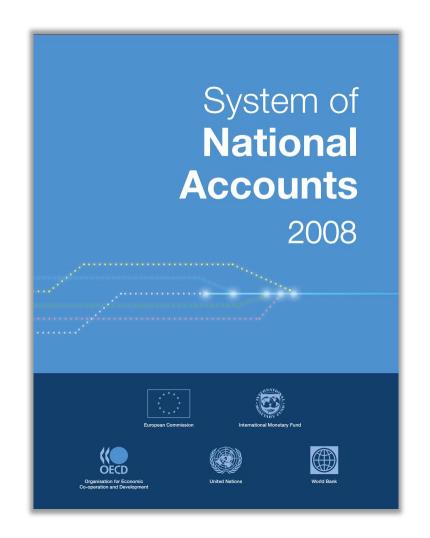


# Part 2

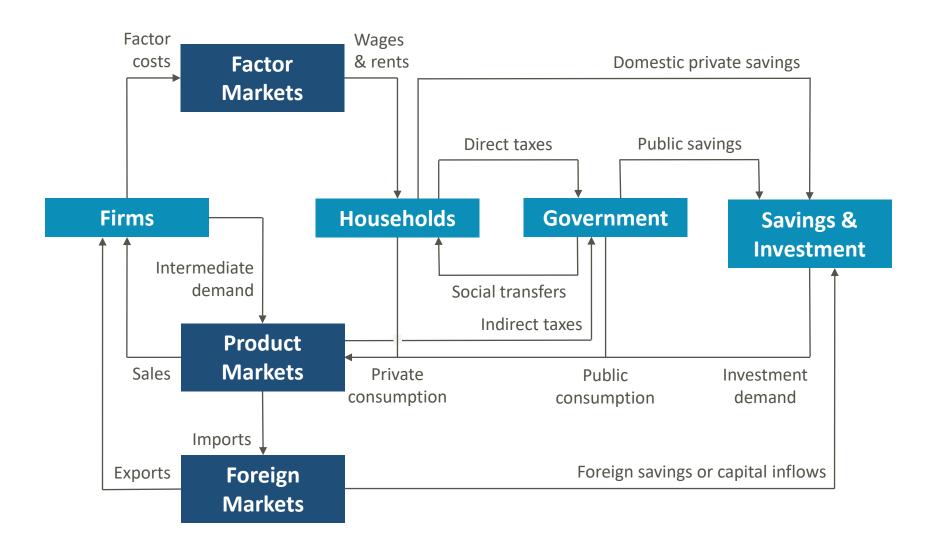
Social Accounting Matrices (SAMs)

## What Is a SAM?

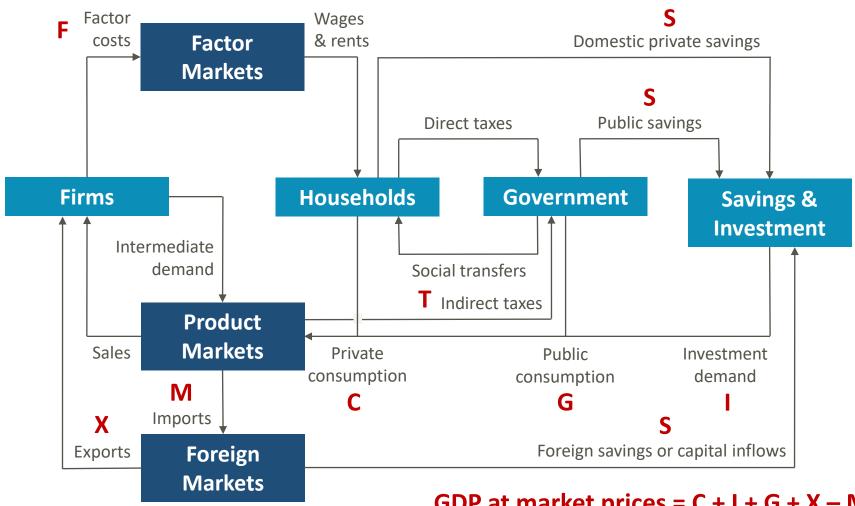
- SAMs are national accounting frameworks or databases
- SAMs capture the circular flow of receipts and payments between economic agents and markets during a given year
- SAMs include all sectors, factors, households, government and the rest of the world (i.e., economywide)
- Every payment becomes someone else's income (i.e., consistent double-entry accounting)



## Circular Flow



## Accounting Indentities



GDP at market prices = C + I + G + X - M

**Total Investment I = Total Savings S** 

**GDP** at market prices = **GDP** at factor cost F + Indirect Taxes T

## **SAM Structure**

Incomes across rows

Expenditures down columns

	ACT	СОМ	FAC	HHD	GOV	INV	ROW	ТОТ
ACT		Marketed output						Activity incomes
СОМ	Intermediate demand			Private consumption	Public consumption	Investment demand	Exports	Total demand
FAC	Value added							Factors incomes
HHD			Income distribution		Social transfers		Remittances	Household incomes
GOV	Producer taxes	Tariffs, VAT & excise taxes		Direct taxes			Foreign aid	Government revenues
SAV				Private savings	Public savings		Foreign savings	Total savings
ROW		Imports	Repatriated profits		Debt repayments			Foreign payments
тот	Gross output	Total supply	Factor payments	Household expenditures	Government expenditures	Total investment	Foreign receipts	

## Macro SAM | Data Sources

- Three main data sources:
  - National Accounts (activity and commodity accounts)
  - Government Financial Statistics (spending and tax accounts)
  - Balance of Payments (external account)
- Standardized concordance between SAM and classification systems
  - GFS2014 & BOP6 → SNA 2008 → Macro SAM accounts
- Inconsistent values across sources requires reconciliation:
  - Consistency with national accounts usually afforded highest priority, followed by BOPs and then GFS

## Macro SAM | Entries

Incomes across rows

Expenditures down columns

	Act	Com	Fact	Ent	Hhd	Gov	Tax	S-I	Stk	Wld	Tot
Activities		NA									NA
Commodities	NA				NA	NA		NA	NA	NA	NA
Factors	NA									ВОР	X
Enterprises			X			GFS				ВОР	X
Households			X	X		GFS				ВОР	X
Government			GFS	GFS	GFS		GFS			ВОР	GFS
Taxes	NA	NA	GFS	GFS	GFS						GFS
Savings				?	X	GFS				ВОР	X
Stock change								NA			X
Rest of world		NA	ВОР	ВОР	ВОР	ВОР					ВОР
Total	NA	NA	X	X	X	GFS	GFS	NA	NA	ВОР	

NA National AccountsGFS Government Financial Statistics

BOP Balance of PaymentsX Convention or residual

# Macro SAM | Details

Incomes across rows

Expenditures down columns

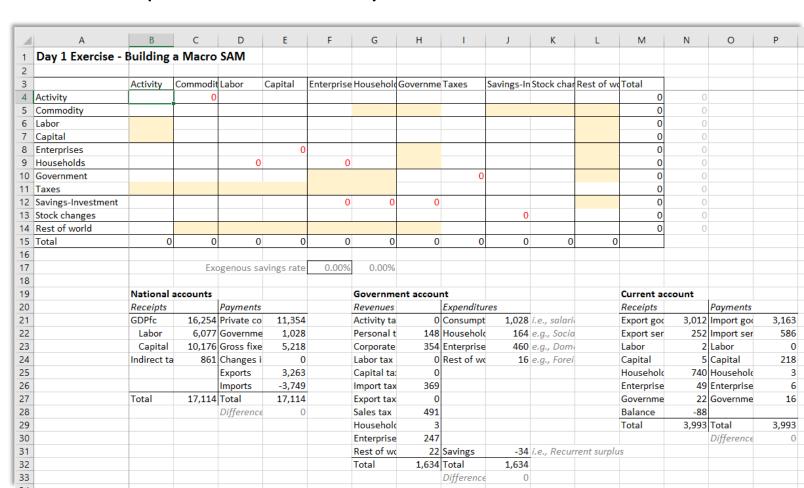
	Act	Com	Fact	Ent	Hhd	Gov	Tax	S-I	Stk	Wld	Tot
Activities											
Commodities											
Factors	Fac	tors									
Enterprises		r   Land	d I Can	ital							
Households	Labo	ı   Lain	u   Cap	Itai							
Government											
Taxes	Tax	es									
Savings		rities (p	roduce	r)   Exr	ort dut	ies I In	nport				
Stock change		es   Sale					.,,				
Rest of world											
Total											

## **Exercise 1** | Building a Macro SAM

- Complete the Macro SAM using the data provided below
  - Yellow cells need data from the tables
  - Red numbers contain formulas that will update automatically

Exercises folder

Exercise 1 - Macro SAM.xlsx



# Supply-Use Table | Details

Incomes across rows

Expenditures down columns

	Act	Com	Fact	Ent	Hhd	Gov	Tax	S-I	Stk	Wld	Tot
Activities		96	activit	tios 4	96 cc	mma	ditio				
Commodities		80 6	activi	иез т							
Factors											
Enterprises											
Households											
Government											
Taxes											
Savings											
Stock change											
Rest of world											
Total											

IFPRI Standard NEXUS SAM structure Individual countries may vary

## Supply-Use Table | Accounts

#### Agricultural activities/commodities

Maize | Sorghum + millet | Rice | Wheat + barley | Other cereals | Pulses | Groundnuts | Other oilseeds | Cassava | Irish potatoes |

Sweet potatoes | Other roots | Leafy vegetables | Other vegetables | Sugarcane | Tobacco | Cotton + fibers | Nuts | Bananas + plantains |

Other fruits | Tea | Coffee | Cocoa | Cut flowers | Rubber | Other crops | Cattle | Raw milk | Poultry | Eggs | Sheep + goats |

Other livestock | Forestry | Aquaculture | Capture fisheries

#### Industrial activities/commodities

Coal | Crude oil | Natural gas | Other mining | Meat | Fish + seafood | Dairy | Fruits + vegetables | Fats + oils | Maize milling |

Sorghum + millet milling | Rice milling | Wheat + barley milling | Other grain milling | Sugar refining | Coffee processing | Tea processing |

Other foods | Animal feed | Beverages | Tobacco | Cotton yarn | Textiles | Clothing | Leather + footwear | Wood | Paper | Petroleum |

Chemicals | Non-metal minerals | Metals + metal products | Machinery | Equipment | Vehicles | Other manufacturing | Electricity + gas |

Water supply + sewage | Construction

#### Service activities/commodities

39

12

Wholesale + retail trade | Transportation + storage | Accommodation | Food services | Information + communication | Finance + insurance | Real estate activities | Business services | Public administration | Education | Health + social work | Other services

IFPRI Standard NEXUS SAM structure Individual countries may vary

## Supply-Use Table | Data Sources

#### Main data sources:

- National accounts (GDP by sector, trade margins)
- Agricultural and industrial production data and surveys
- Input-output table
- Trade and tax data (esp. VAT and customs duties)
- Household expenditure survey (consumption demand vector)

## Standardized concordance between SAM and classification systems

• ISIC3.1, ISIC4, HS2012, COICOP → Disaggregated SAM accounts

## • Inconsistent values across sources requires reconciliation:

Balanced using cross-entropy techniques in GAMS®

# Social Transfers | Details

Incomes across rows

Expenditures down columns

	Act	Com	Fact	Ent	Hhd	Gov	Tax	S-I	Stk	Wld	Tot
Activities											
Commodities	13	facto	rs								
Factors											
Enterprises				15 h	ousel	nolds					
Households											
Government											
Taxes											
Savings											
Stock change											
Rest of world											
Total											

IFPRI Standard NEXUS SAM structure Individual countries may vary

## **Social Transfers** | Accounts

#### **Factors of production**

Crop land | Crop, livestock, mining and nonagricultural capital | Rural and urban labor by education category

#### **Household groups**

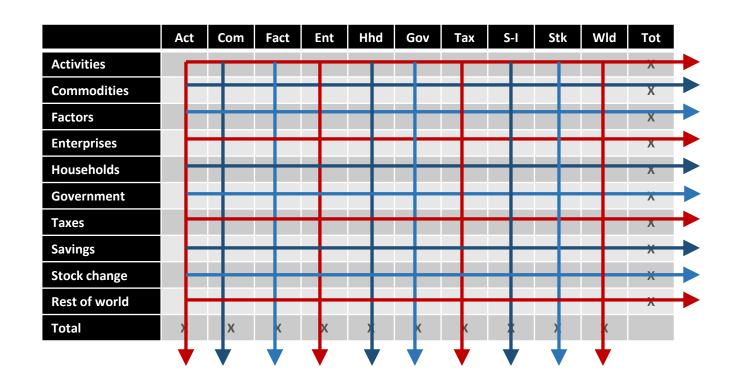
15 Rural farm and nonfarm households and urban households by national per capita expenditure quintiles

## **Social Transfers** | Data Sources

- Main data sources:
  - Household & labor force surveys
- Map sector of employment to Nexus activities
  - ISIC3.1, ISIC4 → Disaggregated SAM accounts
- Map consumption items to Nexus commodities
  - COICOP, etc. → Disaggregated SAM accounts
- Maintain macro SAM and non-factor/household accounts
  - Only imbalances are for detailed household accounts
  - Balanced using cross-entropy in GAMS

## Balancing SAMs | RAS Method

- One approach is to use the RAS method
  - Rows and columns are uniformly scaled in iteration until totals converge
  - Advantages: Simple to implement (even in Excel)
  - **Shortcoming**: Can do significant "damage" to the original data (will adjust cells, even if they are not causing the imbalance)



## Balancing SAMs | Cross-Entropy Method

- Better approach is to use the cross-entropy method
  - Each cell is adjusted individually (rather than entire rows & columns)
  - Minimize deviation from original data (using error distributions)
  - Advantages: Focus more on cells that are causing imbalances
  - **Shortcoming**: More complex (need GAMS rather than just Excel)

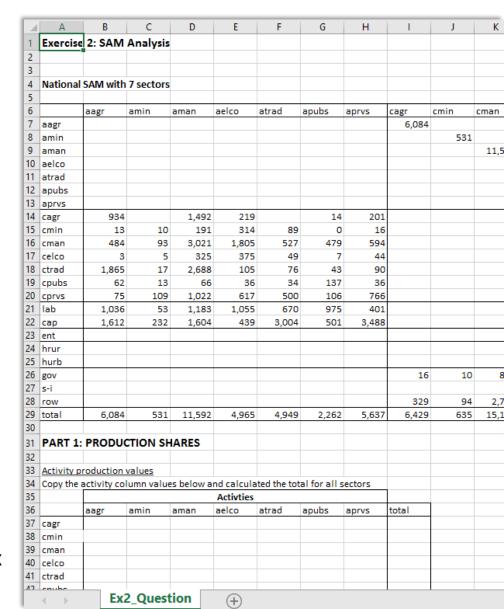
	Act	Com	Fact	Ent	Hhd	Gov	Tax	S-I	Stk	Wld	Tot
Activities						_					X
Commodities											Х
Factors											Х
Enterprises											Х
Households											Х
Government											Х
Taxes											Х
Savings											Х
Stock change											Х
Rest of world											Х
Total	Х	Х	Х	Х	Х	Х	Х	Х	Х	Х	

## Exercise 2 | SAM Analysis

- Aggregated SAM
  - 7 activities, 7 commodities
  - 2 households (rural & urban)
- Answer questions about the structure of the economy
  - Link to data in the SAM
  - Check your answers as you go (correct values shown in blue)

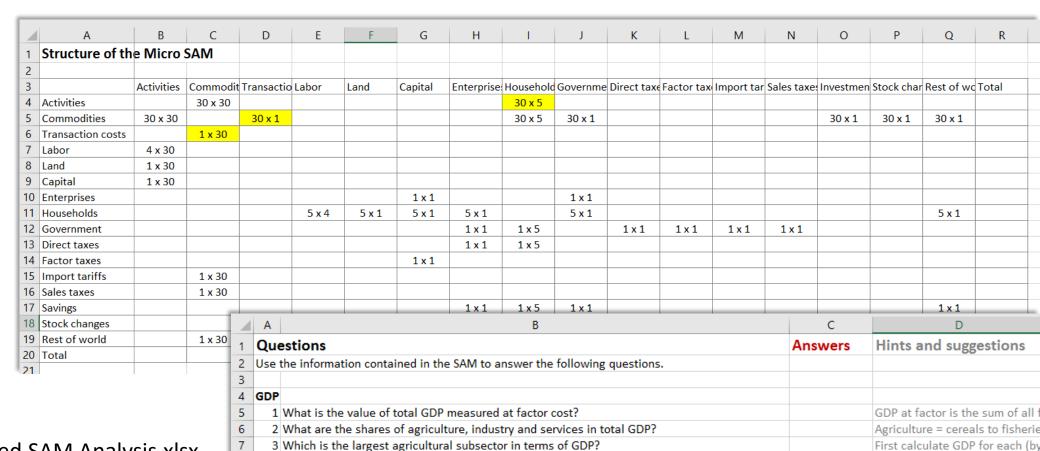
**Exercises folder** 

Exercise 2 – SAM Analysis.xlsx



## Exercise 2x | Detailed SAM Analysis

- Answer the questions using data from the data
  - Use the workings sheet for calculations



4 What is the share of food and agriculture-related processing within manufacturing GDP?

GDP mp = C + I + G + X - M

5 What is the share of the government (incl. health and education) in total GDP?

6 What is the value of GDP measured at market prices?

#### **Exercises folder**

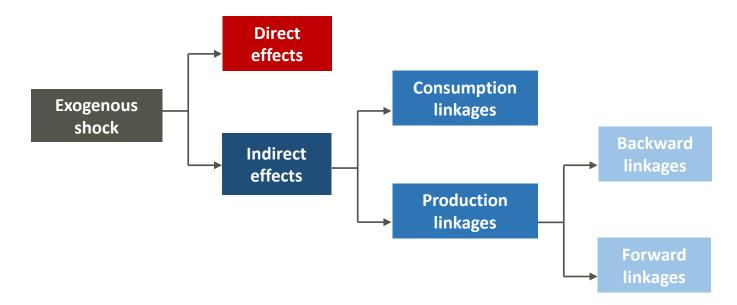
Exercise 2x – Detailed SAM Analysis.xlsx



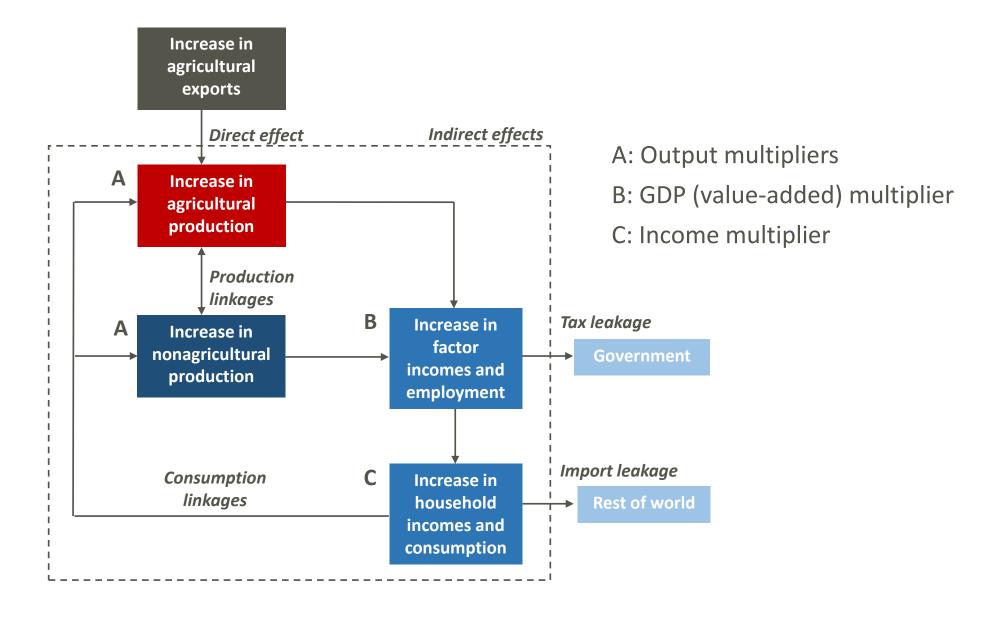
# Part 3 SAM Multiplier Analysis

## Direct and Indirect Linkages

- Total impact of demand shock = Direct effects + Indirect effects
- Indirect effects = Production linkages + Consumption linkages
  - Consumption linkages: incomes → demand for other sectors' products
- Production linkages = Backward linkages + forward linkages
  - Backward linkages: producers purchase of inputs from other sectors
  - Forward linkages: supply of upstream producers with intermediate inputs



## Circular Income Flow in Multiplier Process

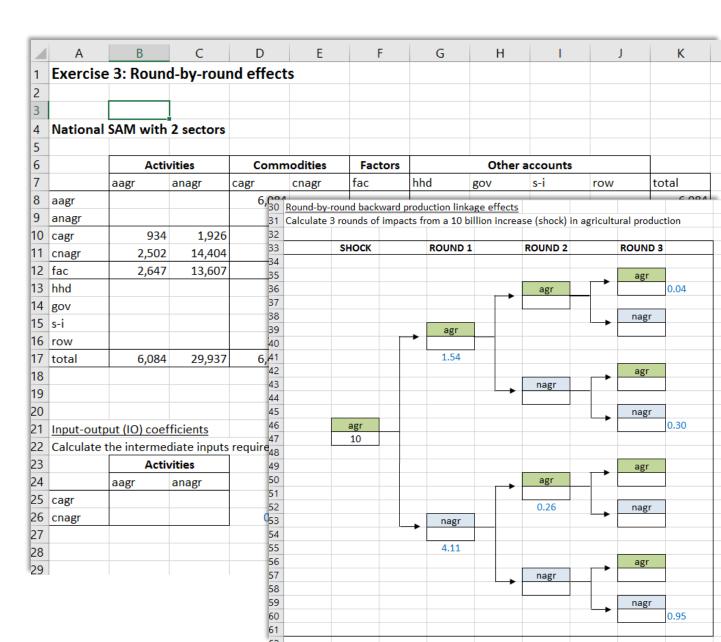


## **Exercise 3** | Round-By-Round Effects

- Manually calculate indirect effects
  - Backward production linkages only
  - 3 rounds of effects
- Check calculations as you go (blue)

#### **Exercises folder**

Exercise 3 – Round-By-Round Effects.xlsx



## Key Assumptions for Multipliers

- Three assumptions behind multipliers...
  - **Fixed prices**: Any changes in demand lead to changes in physical output rather than prices.
  - Unlimited resources: Factor supplies are unconstrained, so that any increase in demand is matched by increased supply.
  - **Fixed input coefficients**: Production technologies and households' consumption patterns are unaffected by exogenous changes in demand (i.e., linkage effects are linear and there is no behavioral change).

## SAM Entries Using Letters or Symbols

We can replace the values appearing in the SAM with letters so that we can use them in deriving the multiplier formula...

	Activities		Comm	odities	Factors	House- holds	Exogenous demand	Total
	A1	A2	C1	C2	F	Н	E	
A1			X <sub>1</sub>					$X_1$
A2				$X_2$				$X_2$
C1	Z <sub>11</sub>	Z <sub>12</sub>				$C_1$	E <sub>1</sub>	$Z_1$
C2	Z <sub>21</sub>	Z <sub>22</sub>				$C_2$	E <sub>2</sub>	$Z_2$
F	$V_1$	$V_2$						V
Н					$V_1 + V_2$			Υ
E			L <sub>1</sub>	L <sub>2</sub>		S		E
Total	X <sub>1</sub>	X <sub>2</sub>	$Z_1$	$Z_2$	V	Υ	E	

 $X = gross output of each activity (i.e., <math>X_1$  and  $X_2$ )

 $Z = total demand for each commodity (i.e., <math>Z_1$  and  $Z_2$ )

V = total factor income (equal to household income)

Y = total household income (equal to total factor income)

E = exogenous components of demand (i.e., government, investment & exports)

# Coefficient Matrix (M)

We then divide each column through by its column total to derive a coefficients matrix (called "M-matrix")...

	Activities		Commodities		Factors	House- holds	Exogenous demand	Total
	A1	A2	C1	C2	F	Н	E	
A1			$b_1 = X_1/Z_1$					$X_1$
A2				$b_2 = X_2/Z_2$				$X_2$
C1	a <sub>11</sub> =Z <sub>11</sub> /X <sub>1</sub>	a <sub>12</sub> =Z <sub>12</sub> /X <sub>2</sub>				$c_1 = C_1/Y$ $c_2 = C_2/Y$	E <sub>1</sub>	$Z_1$
C2	a <sub>21</sub> =Z <sub>21</sub> /X <sub>1</sub>	a <sub>22</sub> =Z <sub>22</sub> /X <sub>2</sub>				$c_2 = C_2/Y$	E <sub>2</sub>	$Z_2$
F	$v_1 = V_1 / X_1$	$v_2 = V_2 / X_2$						V
Н					1			Υ
E			$I_1 = L_1/Z_1$	$I_2 = L_2/Z_2$		s = S/Y		E
Total	1	1	1	1	1	1	E	

- a = technical coefficients (i.e., input or intermediate shares in production)
- b = share of domestic output in total demand
- v = the share of value-added or factor income in gross output
- I = share of the value of total demand from imports or commodity taxes
- c = household consumption expenditure shares
- s = household savings rate (i.e., savings as a share of total household income)

# Multiplier Formula (1)

**Total demand Z** in each sector is the sum of intermediate input demand, household consumption demand, and other **exogenous sources of demand E**...

$$Z_1 = a_{11} X_1 + a_{12} X_2 + c_1 Y + E_1$$

$$Z_2 = a_{21} X_1 + a_{22} X_2 + c_2 Y + E_2$$

From the SAM we know that **gross output X** is only part of total demand Z...

$$X_1 = b_1 Z_1$$
  $X_2 = b_2 Z_2$ 

We also know household income Y depends on factor earnings in each sector...

$$Y=v_1X_1 + v_2X_2 = v_1b_1Z_1 + v_2b_2Z_2$$

We can now replace X and Y in the demand equations...

$$Z_1 = a_{11}b_1 Z_1 + a_{12}b_2 Z_2 + c_1(v_1b_1Z_1 + v_2b_2Z_2) + E_1$$

$$Z_2 = a_{21}b_1 Z_1 + a_{22}b_2 Z_2 + c_2(v_1b_1Z_1 + v_2b_2Z_2) + E_2$$

# Multiplier Formula (2)

From the previous slide...

$$Z_1 = a_{11}b_1 Z_1 + a_{12}b_2 Z_2 + c_1(v_1b_1Z_1 + v_2b_2Z_2) + E_1$$
  
$$Z_2 = a_{21}b_1 Z_1 + a_{22}b_2 Z_2 + c_2(v_1b_1Z_1 + v_2b_2Z_2) + E_2$$

Move all terms, except for exogenous demand E, onto the left-hand side...

$$Z_1 - a_{11}b_1 Z_1 - c_1v_1b_1 Z_1 - a_{12}b_2 Z_2 - c_1v_2b_2 Z_2 = E_1$$

$$-a_{21}b_1 Z_1 - c_2v_1b_1 Z_1 + Z_2 - a_{22}b_2 Z_2 - c_2v_2b_2 Z_2 = E_2$$

Finally, we group Z terms together...

$$(1-a_{11}b_1 - c_1v_1b_1) Z_1 + (-a_{12}b_2 - c_1v_2b_2) Z_2 = E_1$$

$$(-a_{21}b_1 - c_2v_1b_1) Z_1 + (1-a_{22}b_2 - c_2v_2b_2) Z_2 = E_2$$

# Multiplier Formula (3)

From the previous slide...

$$(1-a_{11}b_1 - c_1v_1b_1) Z_1 + (-a_{12}b_2 - c_1v_2b_2) Z_2 = E_1$$

$$(-a_{21}b_1 - c_2v_1b_1) Z_1 + (1-a_{22}b_2 - c_2v_2b_2) Z_2 = E_2$$

We can now use matrix algebra to convert the equations into matrix format...

$$\begin{pmatrix} 1 - a_{11}b_1 - c_1v_1b_1 & -a_{12}b_2 - c_1v_2b_2 \\ -a_{21}b_1 - c_2v_1b_1 & 1 - a_{22}b_2 - c_2v_2b_2 \end{pmatrix} \begin{pmatrix} Z_1 \\ Z_2 \end{pmatrix} = \begin{pmatrix} E_1 \\ E_2 \end{pmatrix}$$

The first term is the identity matrix (I) minus the coefficient matrix (M). We can also rename the other two vectors Z and E...

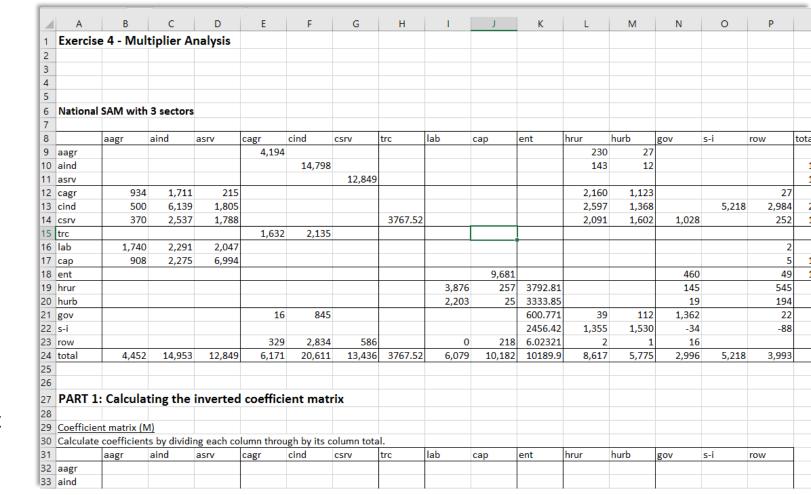
$$(I-M)Z = E$$

Finally, by rearranging terms, we arrive at the unconstrained multiplier formula....

$$Z = (I - M)^{-1} E$$

## Exercise 4 | Multiplier Analysis

- Estimate multiplier effects from an exogenous increase in demand
  - Will need multiplier functions MINVERSE and MMULT (CTRL+SHIFT+ENTER)



#### **Exercises folder**

Exercise 4 – Multiplier Analysis.xlsx

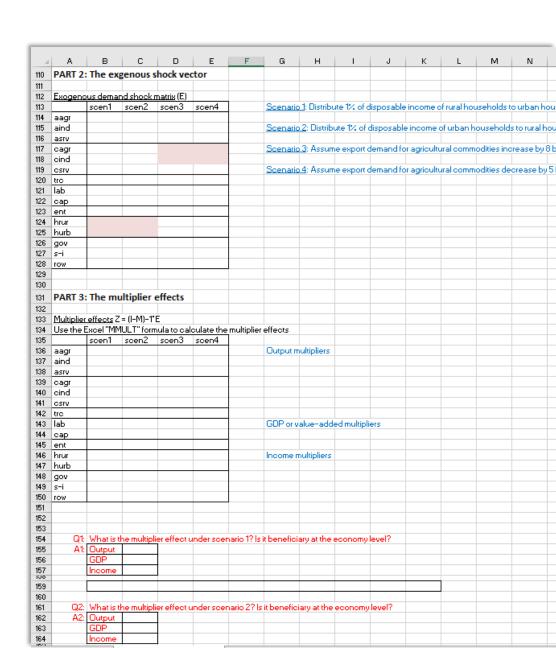
## Exercise 4x | Multiplier Scenarios

 Same SAM and multiplier model from Exercise 4

- Run four simulations
  - 1 & 2: Redistribute rural and urban incomes
  - 3 & 4: Changes in agricultural export demand

**Exercises folder** 

Exercise 4x – Multiplier Scenarios.xlsx

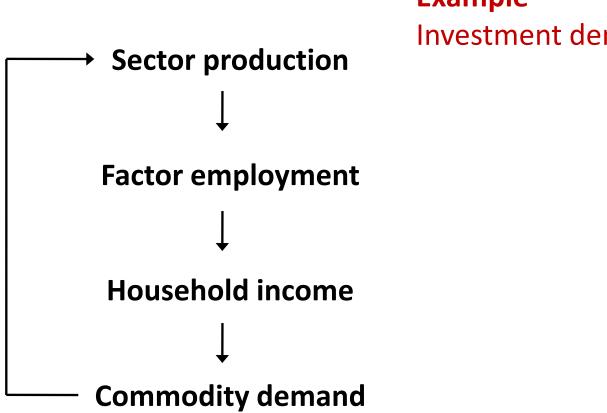




# Part 4 Simple CGE Model

# Tracing an Economic Shock

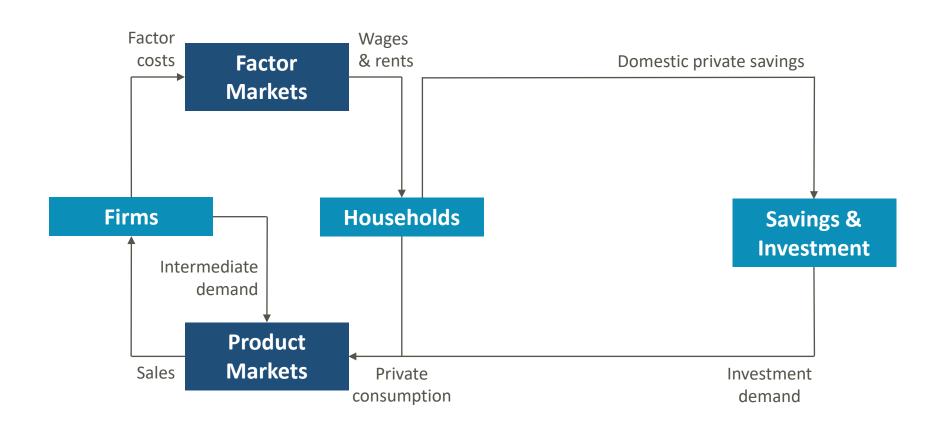
• Using the SAM, we can trace economywide effects of production and demand changes



## **Example**

Investment demand doubles

# Closed-Economy, No Government



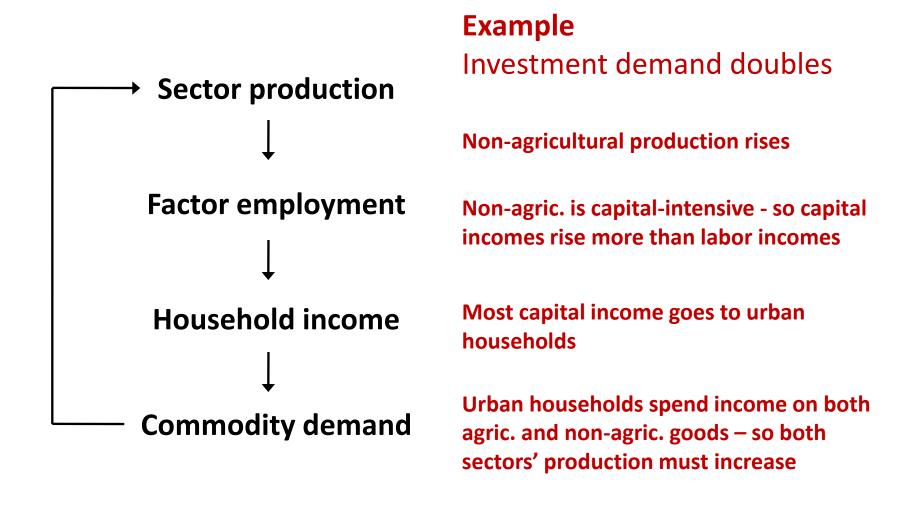
# Simple SAM

Incomes across rows

			A	СТ	CC	OM	FA	<b>NC</b>	HHD		1017	тот
			AG	NAG	AG	NAG	LAB	CAP	RUR	URB	INV	TOT
	ACT	AG			60		0.66	0.40				60
Expenditures	ACT	NAG				50	0.33	0.40				50
down columns	СОМ	AG			0.66	0.40		0.20	40	20		60
1	COIVI	NAG			0.33	0.60	1.00	1.00	20	20	10	50
•	<b></b>	LAB	40	20	1.00	1.00			0.66	0.40		60
	FAC	CAP	20	30	1.00	1.00			0.33	0.60		50
	HHD	RUR					40	20	1.00	1.00		60
	ппи	URB					20	30				50
	SA	<b>N</b>								10		10
	TC	)T	60	50	60	50	60	50	60	50	10	

## Tracing an Economic Shock

• Using the SAM, we can trace economywide effects of production and demand changes



# Tracing Direct and Indirect Effects

Incomes across rows

			A	СТ	C	OM	FA	/C	Н	HD	INV	ТОТ
			AG	NAG	AG	NAG	LAB	CAP	RUR	URB	IINV	101
	ACT	AG			60		0.66	0.40				60
Expenditures	ACI	NAG				60	0.33	0.40				60
down columns	СОМ	AG			0.66	0.40		0.20	42.6	22.25		60
	COIVI	NAG					1.00	1.00	21.8	22.25	20	60
•		LAB	40	24	0.33	0.60						64
	FAC	CAP	20	36	1.00	1.00			0.66	0.40		56
		RUR					42.4	22	0.33	0.60		64.4
	HHD	URB					21.6	34	1.00	1.00		55.6
	SA	AV								11.1		10
	T	OT	60	60	60	60	64	56	64.4	55.6	10	

# Why Do We Need a Model?

- Even for a simple aggregate SAM, tracing the economywide impact of a shock quickly becomes complex
  - In our example, we stopped before second-round effects got started
  - We assumed no resource competition (i.e., production is unconstrained)
- CGE models follow the logic of our example, but use equations to capture all structural linkages in the SAM
  - It is more precise and can use much larger and more complex SAMs
  - It captures resource constraints and market competition (i.e., role of prices in allocating labor/capital and agricultural/non-agricultural goods)

## Simple CGE | Activity Production Functions

		ACT		
		AG	NAG	
<b>5</b> 00	LAB	40	20	
FAC	CAP	20	30	
ТОТ		60	50	

Production technologies are from SAM

$$Q_a = \alpha \cdot LAB_a^{\beta_a} \cdot CAP_a^{1-\beta_a}$$

Resources are scarce and there is fixed supply

$$\overline{LABS} = \sum_{a} LAB_{a} \qquad \overline{CAPS} = \sum_{a} CAP_{a}$$

So producers maximize profits while competing for scarce resources (they pay wages and rents equal to the value of labor and capital's marginal product)

$$w = \frac{\beta_a \cdot P_a \cdot Q_a}{LAB_a} \qquad r = \frac{(1 - \beta_a) \cdot P_a \cdot Q_a}{CAP_a}$$

# Simple CGE | Household Incomes and Spending

		F.A	AC .	ТОТ
		LAB	CAP	ТОТ
	RUR	40	20	60
HHD	URB	20	30	50
ТОТ		60	50	

Factor incomes are paid to households based on fixed factor income shares  $(\theta)$ 

$$\sum_{h} \theta_{h}^{LAB} = 1 \qquad \sum_{h} \theta_{h}^{CAP} = 1$$

$$Y_h = \theta_h^{LAB} \cdot \sum_a w \cdot LAB_a + \theta_h^{CAP} \cdot \sum_a r \cdot CAP_a$$

Households save (S<1) and spend remainder on goods (fixed budget shares  $\delta$ ) to maximize utility

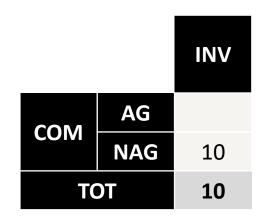
$$P_a \cdot D_{ah} = \delta_{ah} \cdot (1 - S_h) \cdot Y_h$$

$$\sum \delta_{ah} = 1$$

		KUK	UKB
СОМ	AG	40	20
COIVI	NAG	20	20
SA	<b>V</b>		10
ТОТ		60	50

HHD

## Simple CGE | Savings and Investment



In equilibrium, investment demand equals total savings

$$P_a \cdot I_a = \lambda_a \cdot \sum_h S_h \cdot Y_h$$
 
$$\sum_a \lambda_a = 1$$

BUT savings rates (S) and investment (I) cannot both be flexible

We must fix one of these variables...  $\overline{S_h}$  or  $\overline{I_a}$ 

This is a macroeconomic closure rule, which tells the model how to balance the savings-investment account (i.e., should savings drive investment, or should investment drive savings?)

# Simple CGE | Equations & Variables in the Model

$$Q_{a} = \alpha \cdot LAB_{a}^{\beta_{a}} \cdot CAP_{a}^{1-\beta_{a}}$$

$$2eqs = 2vars \quad Q_{a}$$

$$w = \frac{\beta_{a} \cdot P_{a} \cdot Q_{a}}{LAB_{a}} \quad r = \frac{(1 - \beta_{a}) \cdot P_{a} \cdot Q_{a}}{CAP_{a}}$$

$$\overline{LABS} = \sum_{a} LAB_{a} \quad \overline{CAPS} = \sum_{a} CAP_{a}$$

$$2eqs = 2vars \quad w$$

$$r$$

$$Y_{h} = \theta_{h}^{LAB} \cdot \sum_{a} w \cdot LAB_{a} + \theta_{h}^{CAP} \cdot \sum_{a} r \cdot CAP_{a}$$

$$2eqs = 2vars \quad Y_{h}$$

$$P_{a} \cdot I_{a} = \lambda_{a} \cdot \sum_{h} S_{h} \cdot Y_{h}$$

$$2eqs = 2vars \quad or$$

$$I_{a}$$

$$P_{a} \cdot D_{ah} = \delta_{ah} \cdot (1 - S_{h}) \cdot Y_{h}$$

$$4eqs = 4vars \quad D_{ah}$$

## One More Equation

We have equations ensuring that total factor demand equals supply

Total commodity supply  $(Q_q)$  must equal the sum of household and investment demands

$$Q_a = \sum_h D_{ah} + I_a$$

There are two of these equations and two price variables  $(P_a)$  so we are now 'square' (i.e., no. equations = no. endogenous variables)

We need a 'numeraire' = a fixed price against which all other prices are compared to (i.e., acts as a value 'anchor' for the model)

If we fix a variable, we must drop an equation to stay 'square'

## **Model Calibration and Simulation**

- Attach SAM values to the model's parameters and variables
  - SAM is balanced, so model is initially balanced (i.e., in equilibrium)
- When we shock the model, it falls out of equilibrium
  - Solve the model to find a new equilibrium
  - Difference in the values of the variables between the old and the new equilibriums is the impact of the shock (i.e., comparative statics)
- We use the General Algebraic Modeling System (GAMS)
  - GEMPACK is another specialized modeling language/environment

## Extensions in IFPRI Standard CGE Model

## • We use more complicated (flexible) functional forms:

- Constant Elasticity of Substitution (CES) production functions so technologies change with relative factor prices
- Linear Expenditure System (LES) of demand systems to allow for non-unity income elasticities

## Include government and the rest of the world

- CES and CET trade functions allow producers and consumers to shift between domestic and foreign markets
- We also have two extra macro-closures
- Government: Flexible tax rates or spending?
- Current account: Flexible exchange rate or deficit?



# Part 5 IFPRI Standard CGE Model

## Why Have a Standard Model?

#### Common core model

- Avoid reinventing the wheel
- Quick to get up and running for new countries/SAMs
- Can focus on new analysis rather than lots of programming

#### Versatile

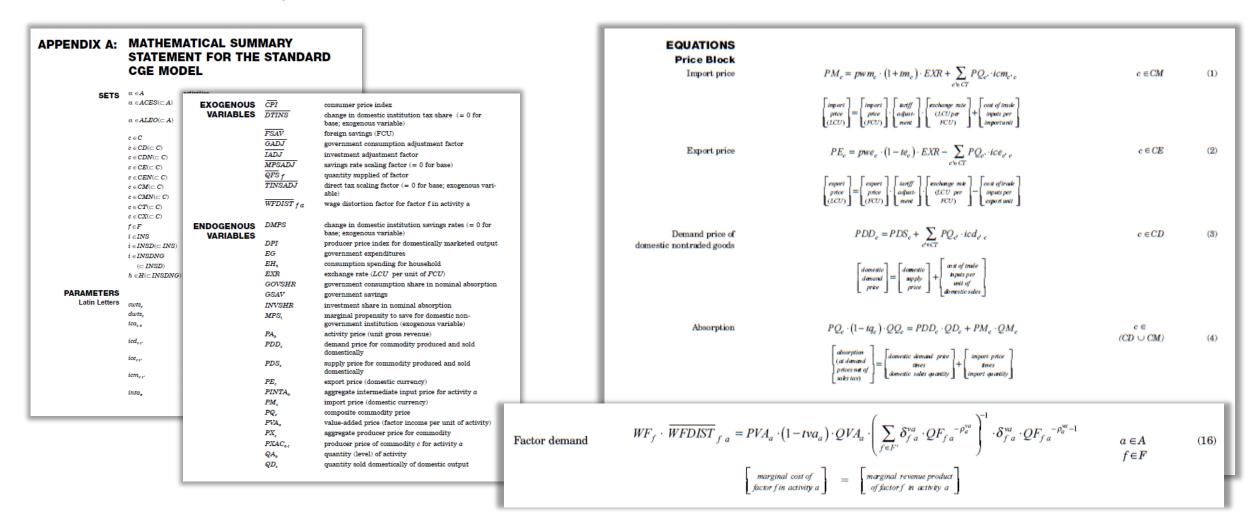
- Captures most unique country characteristics (e.g., taxes)
- Can add complexity or special country characteristics
- Easier to debug or to explain to others what you're doing



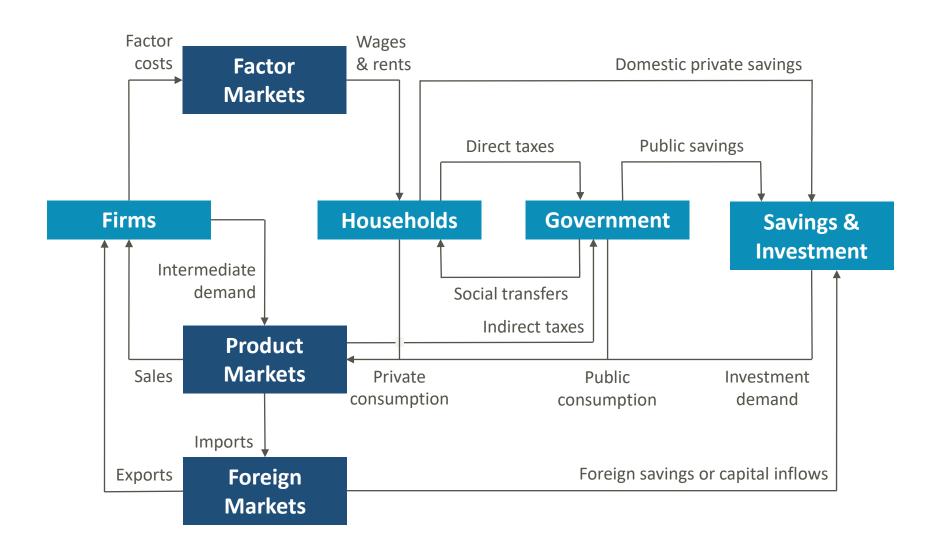
## Too Many Equations, Variables and Parameters!

#### 51 variables & 46 parameters

#### 48 equations



## Flows in the Standard Model



## **Functional Forms**

## **Cobb-Douglas (CD)**

Constant expenditure shares

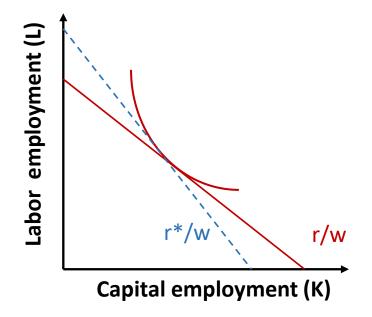
$$Q = \alpha \cdot L^{\beta} \cdot K^{1-\beta}$$

$$w \cdot L = \beta \cdot P \cdot Q$$

$$r \cdot K = (1 - \beta) \cdot P \cdot Q$$

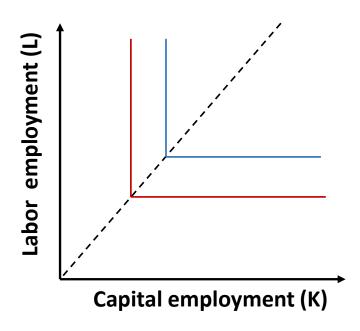
## **Constant Elasticity of Substitution (CES)**

Shares relative to prices



#### Leontief

Fixed quantity ratios



## Linkages vs. Trade-Offs

#### **Basic SAM layout**

	Α	С	F	Н	G	I	w	тот
Α								
С								
F								
Н								
G								
ı								
W								
тот								

**A** = Activities

**C** = Commodities

**F** = Factors

**H** = Households

**G** = Government

l = Investment

W = Rest of world

#### Linkages in the SAM

- Backward & forward production linkages
- Income/demand linkages
- Foreign trade

#### Multiplier models assume unlimited resources

- Implies that prices are fixed
- No trade-offs

#### Resource constraints introduce trade-offs

- Factors are limited = wage rates are set in markets
- Product supply is limited = product prices adjust
- Foreign exchange is limited = exchange rate adjusts

# Supply Chains | Activity Output

#### **Basic SAM layout**

	Α	С	F	D	W	тот
Α						
С						
F						
D						
W						
тот						

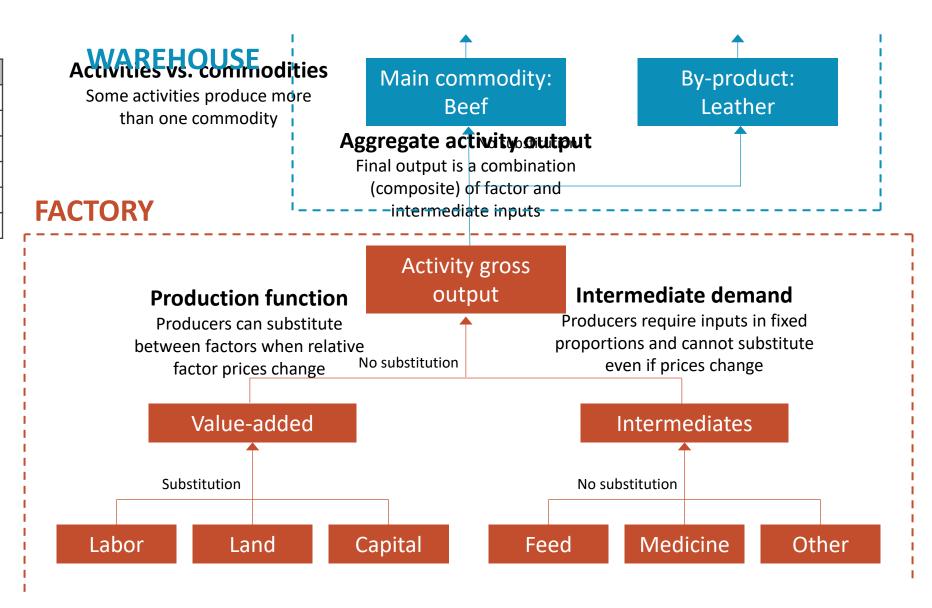
**A** = Activities

**C** = Commodities

**F** = Factors

**D** = Final demanders

**W** = Rest of world



# Supply Chains | Commodity Supply & Demand

Product market closure

Demand & supply balance

maintained via price changes

#### **Basic SAM layout**

	А	С	F	D	w	тот
Α						
С						
F						
D						
w						
тот						

**A** = Activities

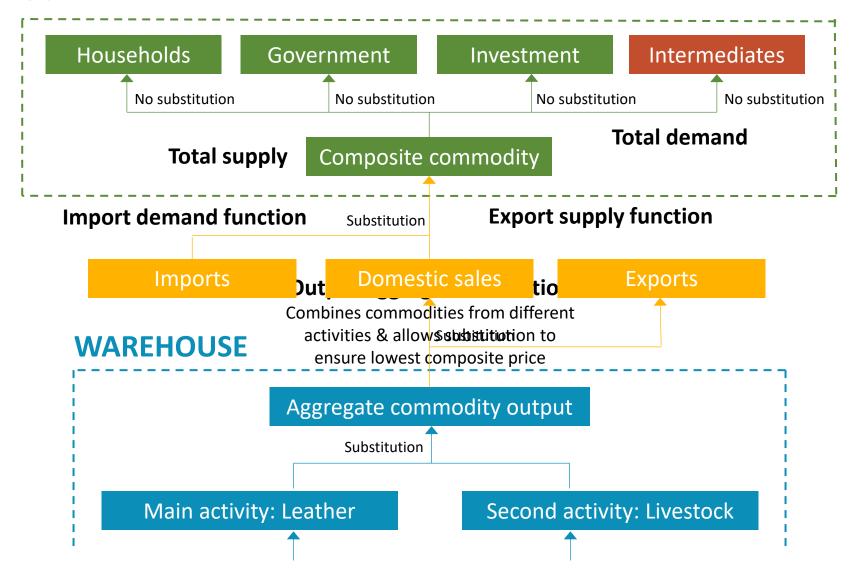
**C** = Commodities

**F** = Factors

**D** = Final demanders

**W** = Rest of world

#### SUPERMARKET



# Supply Chains | Summary

**Equilibrium:** Total commodity supply must equal total demand (mediated by prices changes)

**A** = Activities

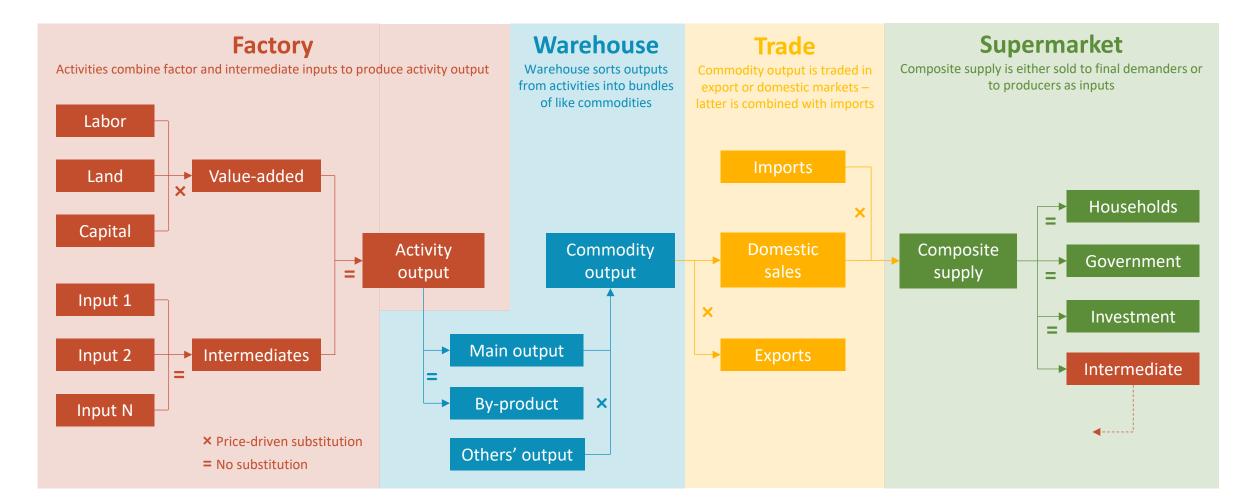
**C** = Commodities

**F** = Factors

D = Final demand

**W** = Rest of world

	Α	С	F	D	w	тот
Α						
С						
F						
D						
w						
тот						



# Supply Chains | Summary

**Equilibrium:** Total commodity supply must equal total demand (mediated by prices changes)

**A** = Activities

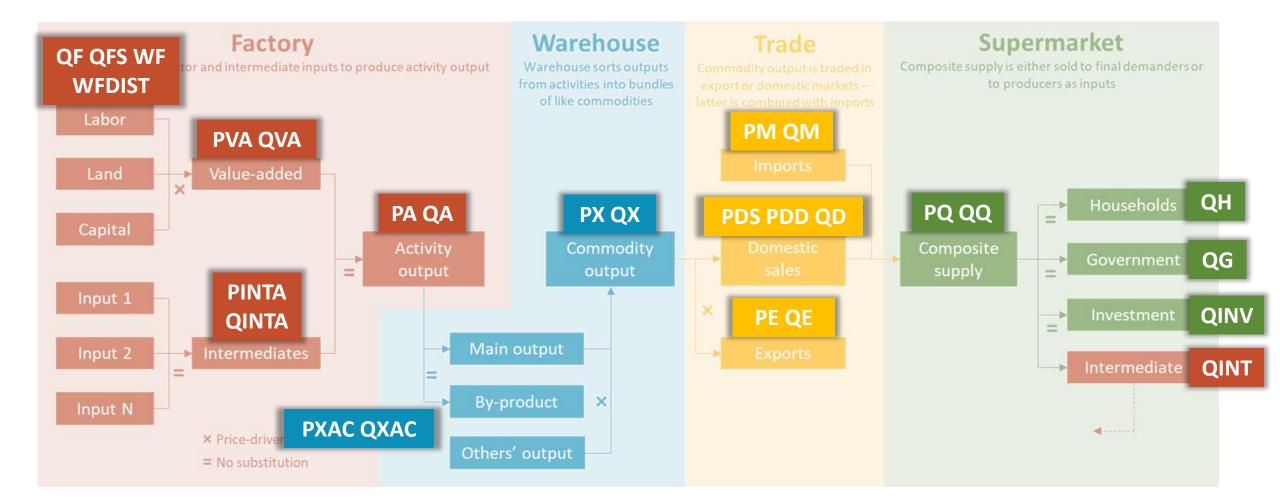
C = Commodities

**F** = Factors

D = Final demand

W = Rest of world

	Α	С	F	D	w	тот
Α						
С						
F						
D						
W						
тот						



## **Factor Markets** | Closure Rules

**Equilibrium:** Total factor supply must equal sum of sectoral factor demand (determined by "closure rules")

**A** = Activities

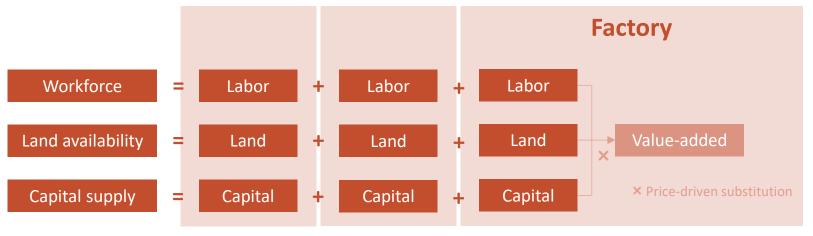
C = Commodities

**F** = Factors

D = Final demand

**W** = Rest of world

	Α	С	F	D	w	тот
Α						
С						
F						
D						
W						
тот						



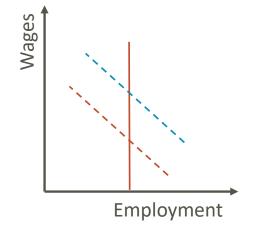
#### Fix one

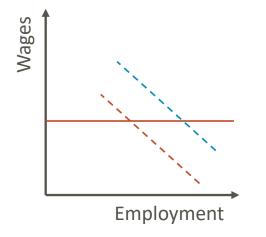
Economywide wage Total factor supply

#### **Factor market closure**

- Adjust total factor supply?
- Adjust wages?



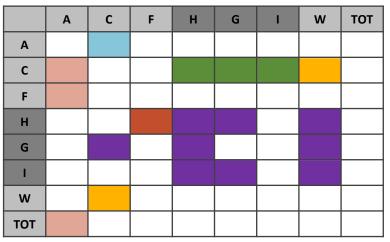




Option 2
Unemployment

## **Institutions** | Incomes & Spending

#### **Basic SAM layout**



**A** = Activities

C = Commodities

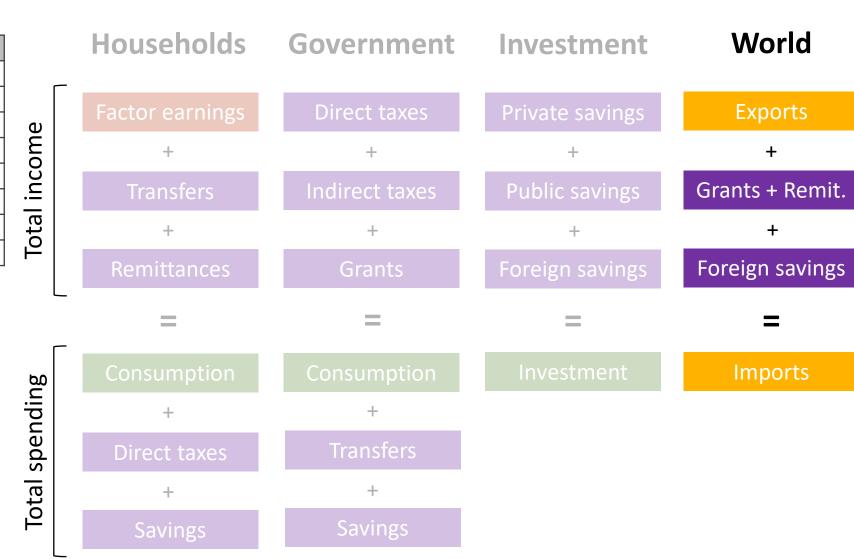
**F** = Factors

**H** = Households

**G** = Government

l = Investment

**W** = Rest of world



## Macroeconomy | Closure Rules

**Equilibrium:** Total receipts must equal total expenditures (determined by "closure rules")

**A** = Activities

C = Commodities

**F** = Factors

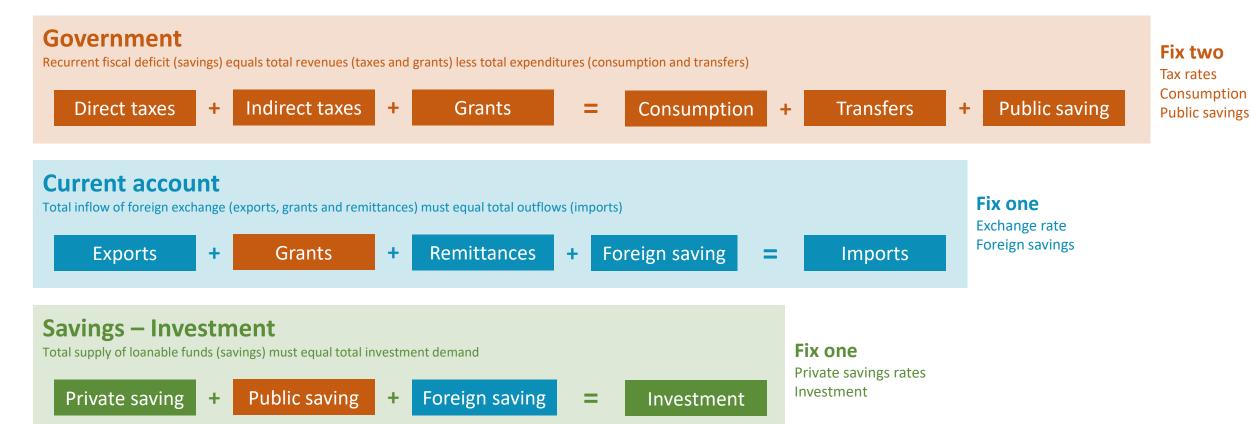
I = Households

= Government

= Investment

**W** = Rest of world

	Α	С	F	Н	G	1	W	тот
Α								
С								
F								
Н								
G								
ı								
w								
тот								



## Standard CGE Model | Key Features

- Capture all economic linkages (based on the SAMs)
- Drop the assumption that resources are unconstrained (i.e., fixed prices, as in multiplier models)
  - Product prices
  - Factor prices (labor wages, land rents, capital profits)
  - Exchange rate
- Maintain macroeconomic & resource balances (no "free lunch")
  - Government fiscal accounts
  - Investment & savings
  - Current account / balance of payments
  - Factor markets
- Provides a consistent framework for tracking economywide impacts
  - Macro-accounting principles are respected (e.g., receipts must equal payments)
  - Macro and micro feedbacks are tracked (e.g., sectors, workers, households)

## Standard CGE Model | Other Features

### Enterprises

- Receive some factor incomes (usually capital)
- Pay taxes (corporate), save, remit
- Pay whatever is left to households (i.e., indirect capital payments)

#### Taxes

- Indirect: Producer taxes, sales taxes, factor taxes, and export taxes
- Direct: Personal income taxes, corporate taxes
- Tax changes can be proportional or point changes

## Change in stocks or inventories

- Residual investment (drawing down or increasing inventories)
- No behavior or effect on savings-investment closure

## Standard CGE Model | Calibration

- Attach values to the model's variables and parameters
- Most data comes directly from the SAM
  - Usually assume that prices are equal to one so quantities are equal to SAM values
- But some data must come from external sources
  - Employment numbers (QF and QFS) non-unitary wages (WF and WFDIST)
  - Household income elasticities for each commodity (budget surveys?)
  - Factor and trade substitution elasticities (GTAP?)



# Part 6

Microsoft-Excel® Interface

## Standard Model

#### IFPRI's standard static model

#### Nexus SAM

- 86 activities & 86 commodities
- 13 factors of production
- 15 household groups

#### National data file sheets

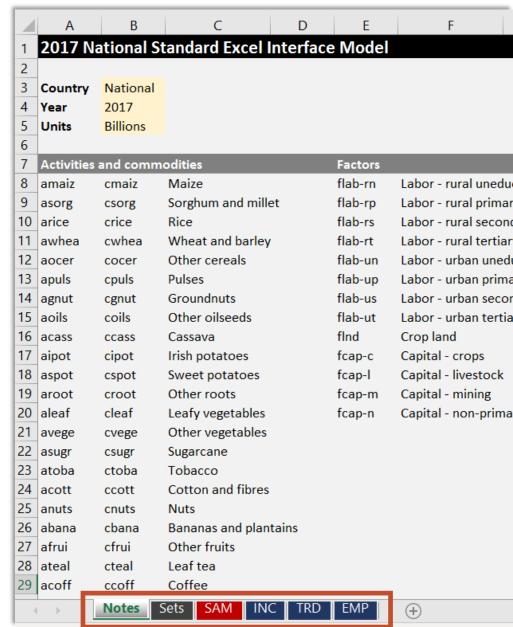
SAM social accounting matrix

• INC income elasticities

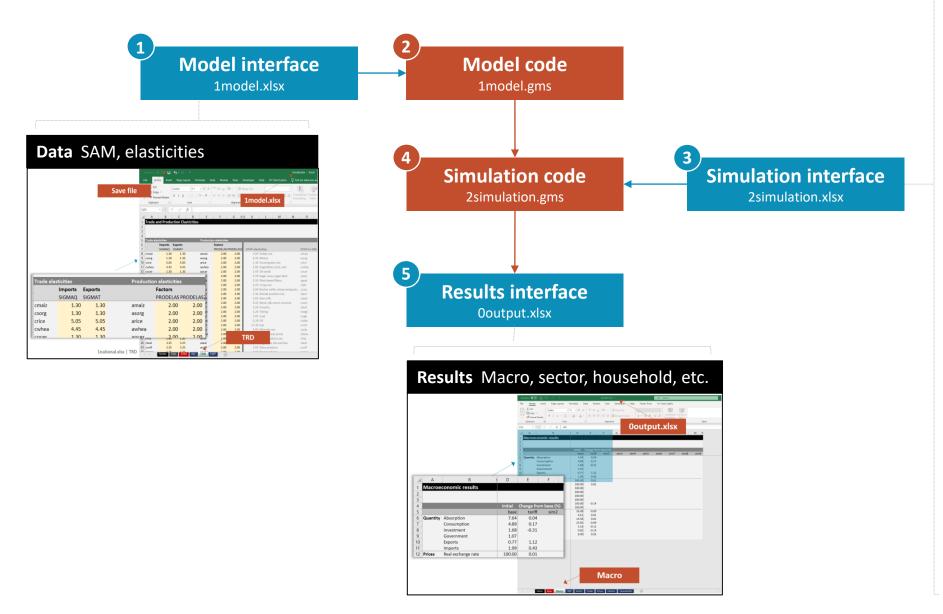
TRD trade/production elasticities

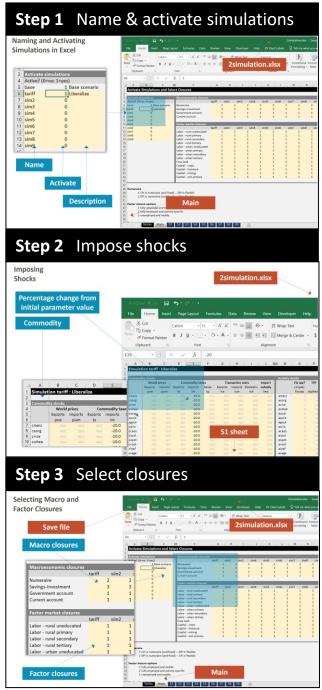
EMP wages & employment

#### 1national.xlsx | Notes

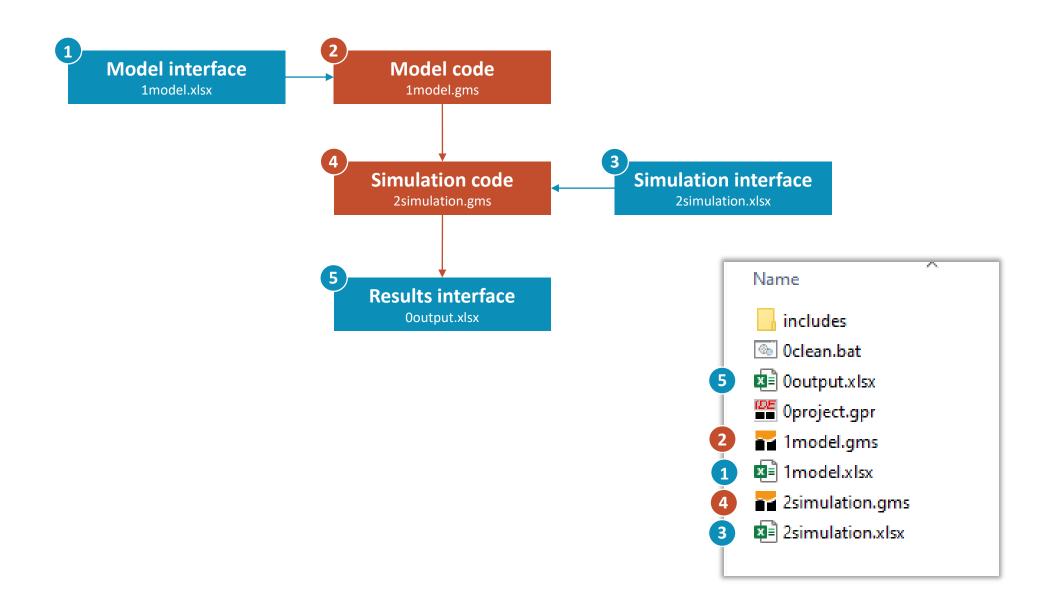


# Five Steps to Running Simulations

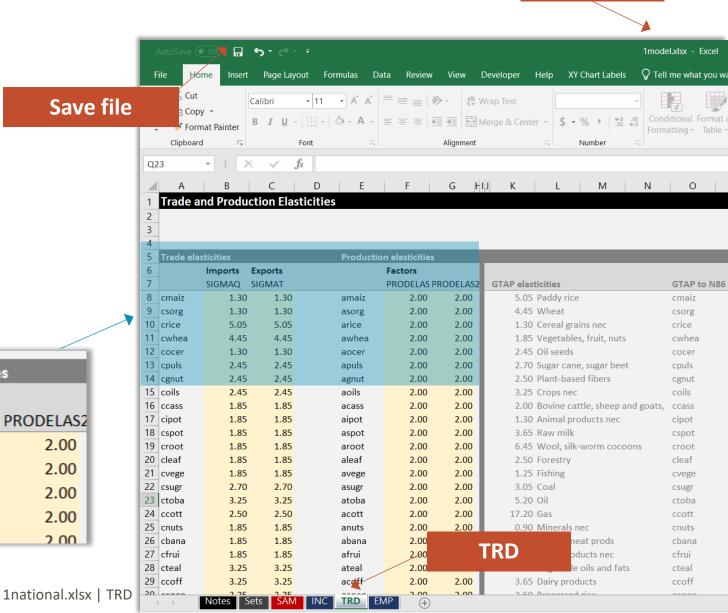




# Files in the Folder



# Step 1 | Changing Elasticities (Optional)

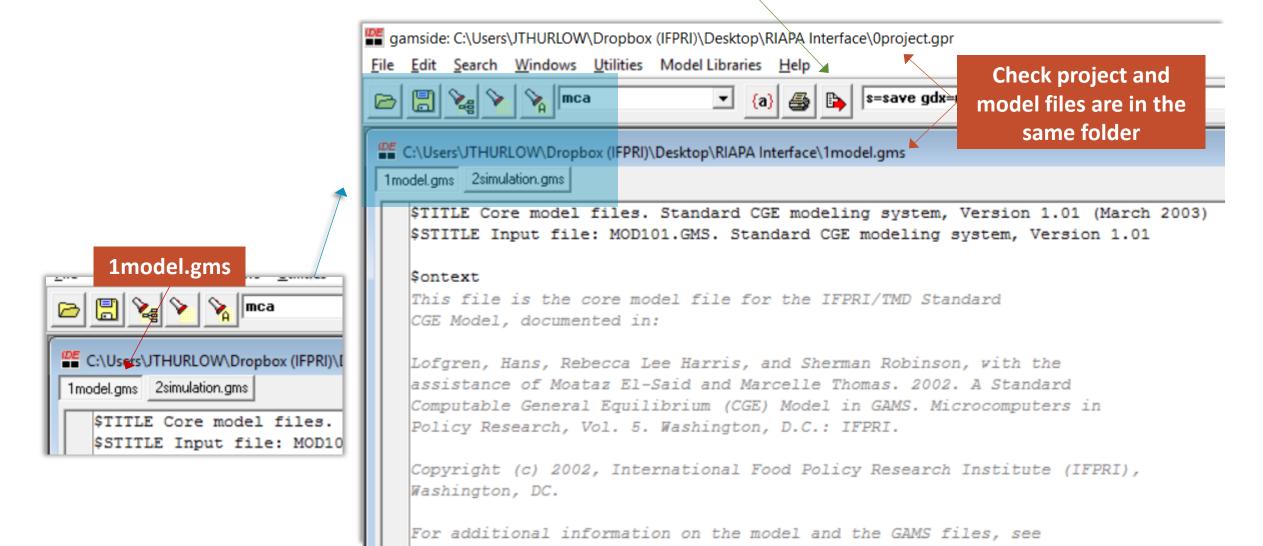


1model.xlsx

Trade elasticities			Production elasticities		
	Imports	Exports		Factors	
	SIGMAQ	SIGMAT		PRODELAS PR	RODELAS2
cmaiz	1.30	1.30	amaiz	2.00	2.00
csorg	1.30	1.30	asorg	2.00	2.00
crice	5.05	5.05	arice	2.00	2.00
cwhea	4.45	4.45	awhea	2.00	2.00
cocer	1 30	1 30	ancer	2.00	2.00

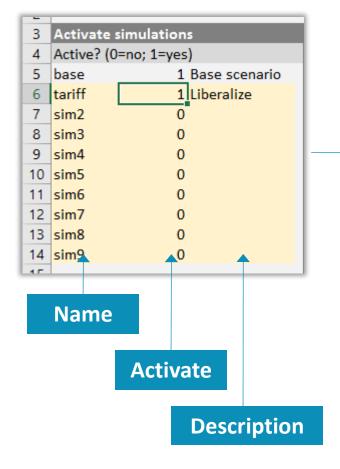
# Step 2 | Initializing Model (Push F9)

#### Press F9

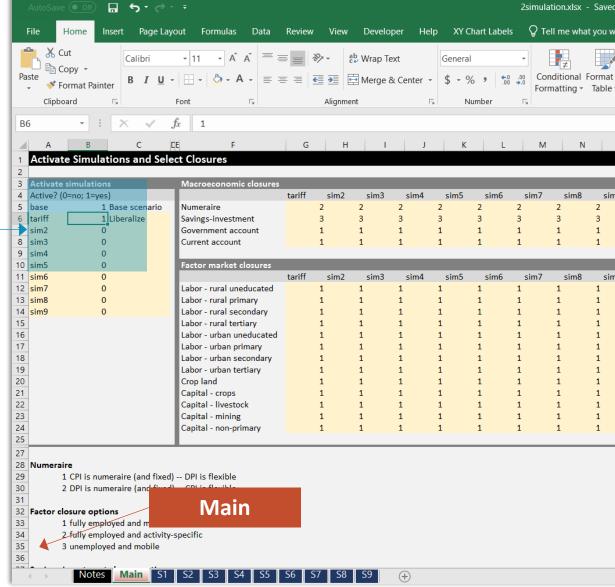


# **Step 3.1** | Designing Simulations

**Naming and Activating Simulations in Excel** 

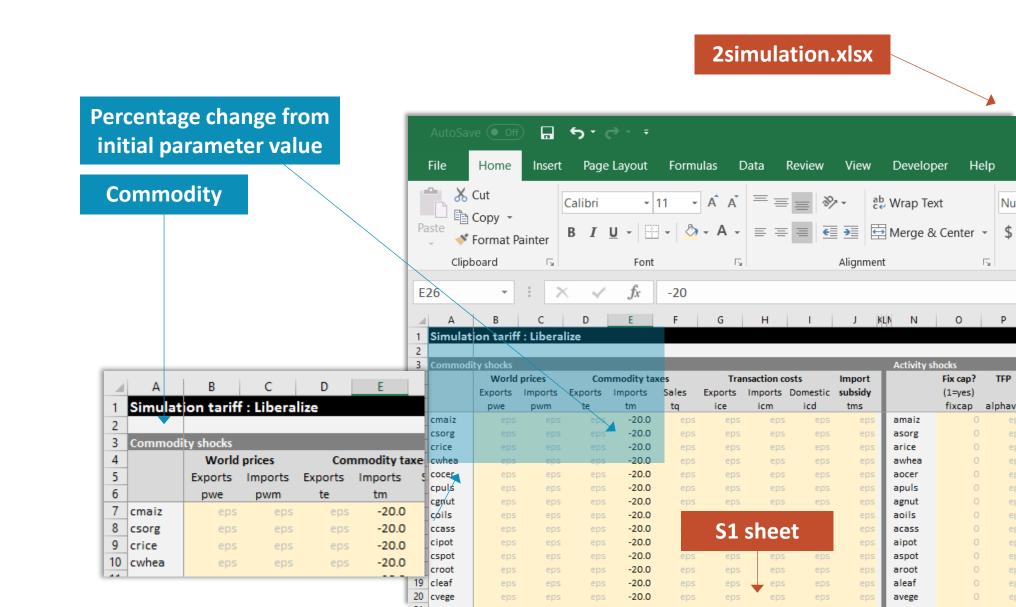






# **Step 3.2** | Designing Simulations

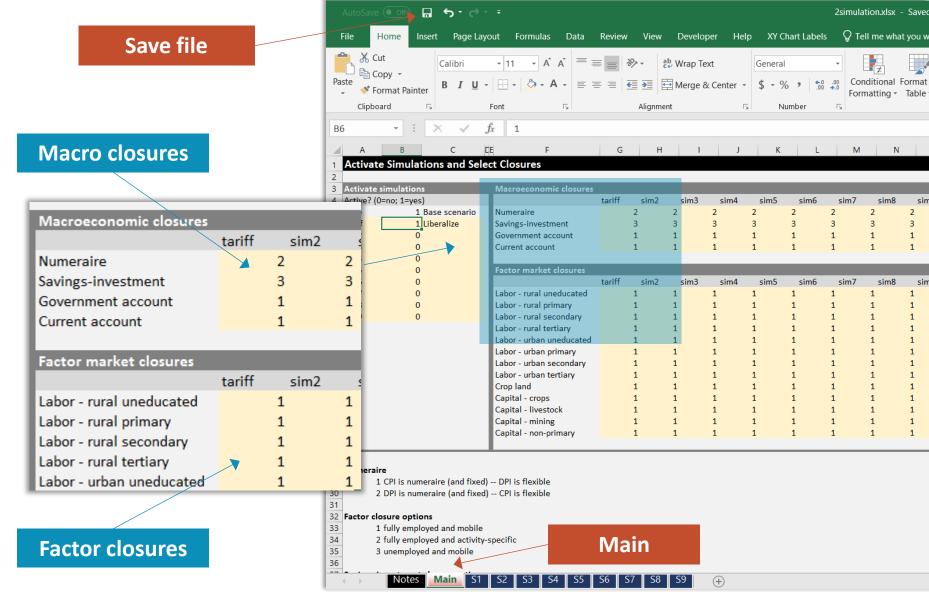
**Imposing Shocks** 



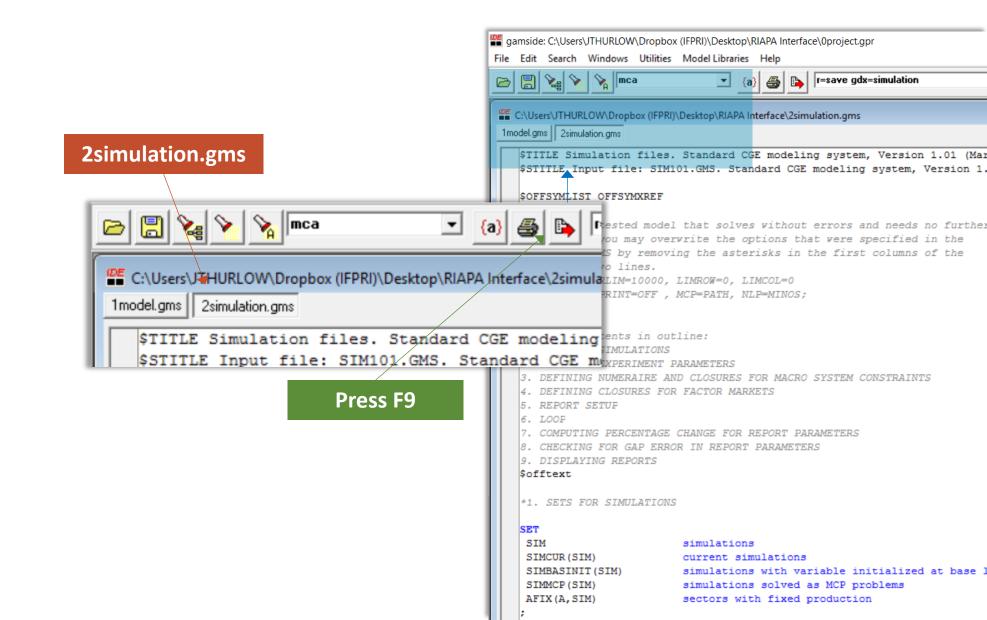
# **Step 3.3** | Designing Simulations

2simulation.xlsx

**Selecting Macro and Factor Closures** 

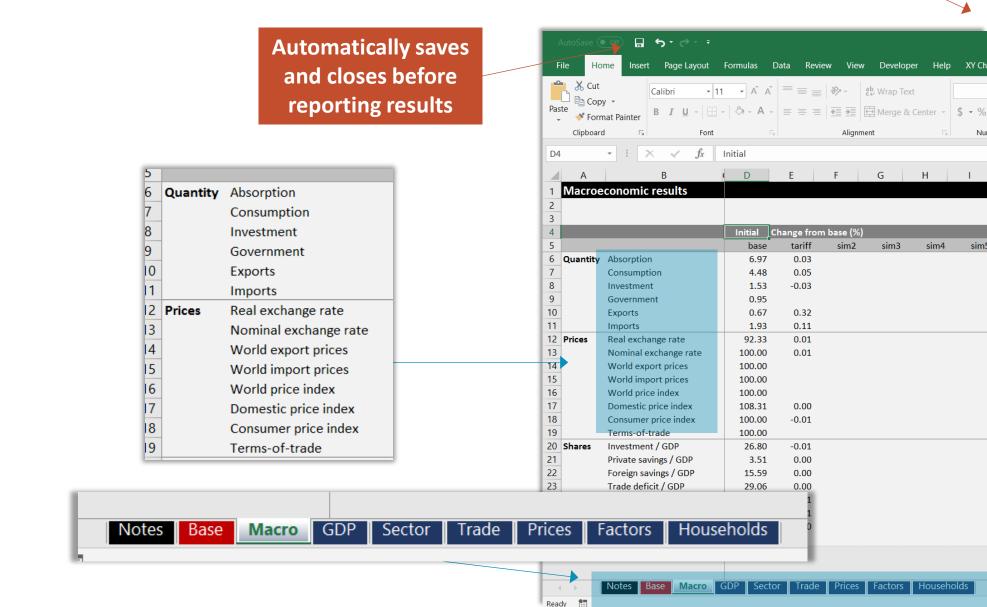


# **Step 4** | Running Simulations (Push F9)



# **Step 5** | Reviewing Simulation Results

Ooutput.xlsx



# **Step 5** | Reviewing Simulation Results

Worksheet	Tables		
Base	Initial sectoral production, trade and tax structure		
Macro	Macroeconomic results, including exchange rates and CPI		
GDP	GDP by expenditure group (nominal and real)		
Sector	Sectoral GDP at factor cost		
Trade	Real value of imports and exports		
Prices	Producer, market and world prices		
Factors	Total factor supply, economy-wide returns, total factor incomes, and sectoral factor demand		
Households	Institutional incomes, equivalent variation (welfare), real expenditure by commodity, and institutional tax rates and collections		

# **Note** | Some Constraints to Using Interface

- To run the interface version of the standard model you need licensed versions of Excel and GAMS (Path)
- You cannot change SAM structure (for this you would need to adapt the interface)
  - BUT you can update the model to a more recent year using the SAM Toolkit
- You cannot add new parameters to the interface
  - BUT all of the existing parameters in the standard model can be shocked using the interface

# Note | Available Shock Parameters

Category	Parameter	Description
Commodity shocks	pwm pwe	World import and export prices
	tm te	Import and export taxes
	tq	Sales taxes
	ice icm icd	Export, import and domestic transaction costs
Activity shocks	alphava	TFP (production function shift parameter)
	ta tva	Activity and value-added taxes
Factor shocks	tf	Factor taxes
	wf	Economywide (average) factor returns
	qfs	Total factor supply
Macroeconomic shocks	exr	Exchange rate
	fsav	Foreign savings (capital inflows)
	gsav	Government savings/deficit
	gadj	Government recurrent expenditures



# Part 6 (continued)

Exercises Using the Interface Model

# **Exercise 5** | Foreign Capital Outflows

## **Shock**

Increase foreign capital outflows fivefold (i.e., +500% foreign savings)

## Four sets of closures

Sim1: Full employment, savings-driven investment

• **Sim2**: Full employment, investment-driven savings

• **Sim3**: Unemployment, investment-driven savings

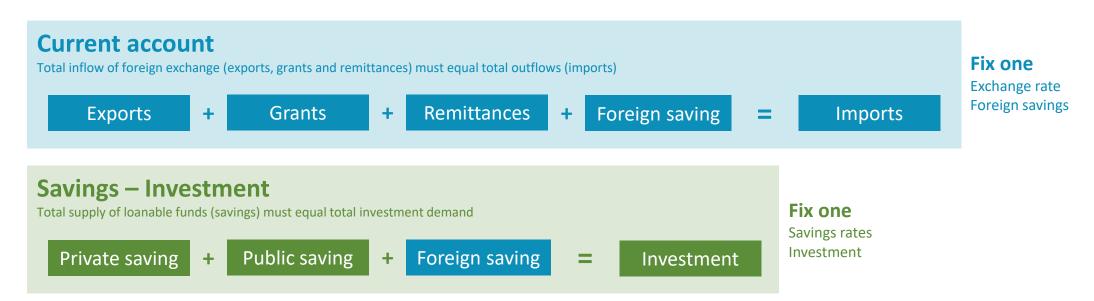
• **Sim4**: Unemployment, investment-driven savings

(fixed savings rates, flexible investment)

(fixed investment, flexible savings rates, scaled MPS adjustment)

(fixed wage rate, flexible labor supply, scaled MPS adjustment)

(fixed wage rate, flexible labor supply, uniform MPS adjustment)



# Exercise 5 | Walkthrough

### Macro

- $\downarrow$  Foreign savings = Exchange shortage  $\rightarrow$  Real exchange rate depreciation  $\rightarrow$   $\uparrow$  Exports &  $\downarrow$  Imports
- $\downarrow$  Foreign savings =  $\downarrow$  Loanable funds  $\rightarrow$   $\downarrow$  Investment OR  $\uparrow$  Private savings

 $\uparrow$ Private savings  $\rightarrow$   $\downarrow$ Private consumption

## Trade (+ Base)

• Depreciation  $\rightarrow$   $\uparrow$ Export-oriented commodities (e.g., flowers) &  $\downarrow$ Import-intensive commodities (e.g., cars)

#### **Sector**

- $\downarrow$ Investment  $\rightarrow$   $\downarrow$ Construction & Mining (i.e., stone, sand, etc.) & Nonmetal minerals (e.g., cement)
- $\downarrow$ Private consumption  $\rightarrow$   $\downarrow$ Food (e.g., crops, livestock, etc.)

#### **Factors**

•  $\downarrow$  Wages OR  $\uparrow \downarrow$  Employment (larger  $\downarrow$  wage with  $\downarrow$  construction, which is capital-intensive)

#### Households

- ↓Private consumption (larger with ↑private savings & unemployment)
- Poor rural households are worst-affected

# **Exercise 6** | Tariff Liberalization

## Shock

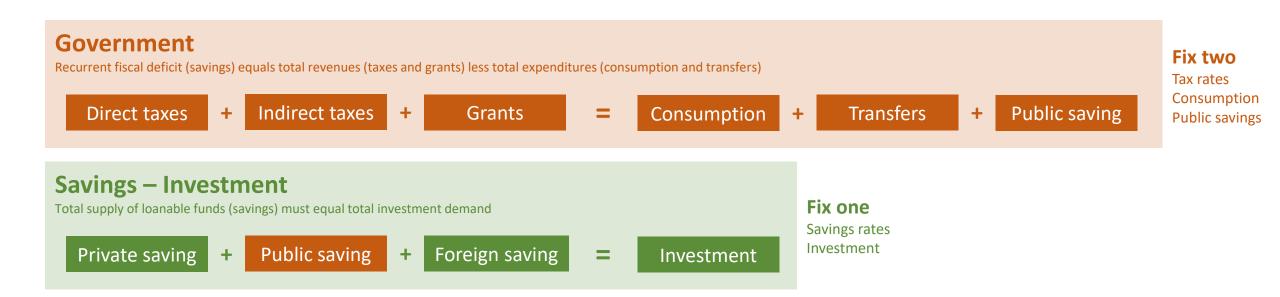
• Eliminate all tariffs (i.e., -100%)

## Two sets of closures

- Sim1: Full employment, savings-driven investment, deficit financed
- **Sim2**: Full employment, savings-driven investment, tax financed

(fixed savings rates, flexible investment, flexible government savings)

(fixed savings rates, flexible investment, flexible direct tax rates)



# Exercise 6 | Walkthrough

#### Macro

↓Tariffs → ↑Imports → Real exchange rate depreciation → ↑Exports
 ↓Tariffs → ↓Consumer prices → ↑Private consumption
 ↓Tariffs = Revenue shortfall → ↓Public savings OR ↑Tax rates
 ↓Public savings → ↓Investment
 ↑Tax rates → Smaller ↑private consumption

## Trade (+ Base)

•  $\sqrt{\text{Tariffs}} \rightarrow \text{Timport-intensive commodities}$ 

#### **Sector**

•  $\downarrow$ Tariffs  $\rightarrow \downarrow$ GDP for import-competing sectors

#### Households

- ↑Private consumption (smaller with ↑private savings)
- $\uparrow$ Tax rates  $\rightarrow$   $\downarrow$ Consumption for high-income urban households

# Group Exercises (1)

## 1. Flooding the fields

Reduce crop productivity (TFP) by 20%

## 2. Running on empty

Increase world oil (petroleum and fertilizer) prices by 30%

## 3. Lights out

Productivity (TFP) in the electricity sector falls by 20%

# 4. Buck stops here

Halve foreign remittance inflows

# 5. Emperor's clothes

World prices for textiles and clothing drop 30%

# Group Exercises (2)

## 6. Saving the planet

• Impose a 50% tax (negative subsidy) on fossil fuel-related imports

## 7. Robin Hood

Double government transfers to poor households (find a way to pay for it)

# 8. Building bridges

Increase capital investment in trade and transport infrastructure

## 9. Filling the coffers

Increase government revenues using different instruments



# Part 7

Extending the Standard Model

# Three Extensions

# Recursive dynamics

Simple dynamic specification

## Microsimulation

Linking to the household survey

## Additional accounts

- Environmental accounts (e.g., natural resources, pollution, etc.)
- Financial accounts (i.e., monetary sector variables)

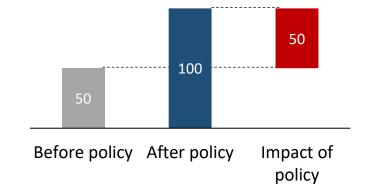
# **Recursive Dynamics** | Counterfactual Analysis

# CGE model is a laboratory for experimenting with different policies and shocks

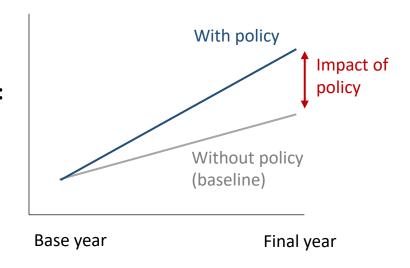
 Counterfactual analysis measures outcomes with (before) and without (after) shock or intervention

# Can be used as either static or dynamic model

 Choice depends on the policy or shock being analyzed (e.g., impacts of a rapid onset shock vs. designing long-term investment strategies) In a static model:



In a dynamic model:



# **Recursive Dynamics** | Annual Updates

## CGE model is solved annually with inter-annual updates to key parameters

- Endogenous updates depend on results from previous years
- Exogenous updates are fixed over time

## **Endogenous Updating**

#### **Capital accumulation rate**

 Depends on previous year's investment levels, which are themselves endogenous (i.e., of national incomes and savings rates)

## **Capital allocation by sector**

 Depends on past investment allocations and previous year's relative profits across sectors

## **Exogenous Updating**

## **Population & labor supply**

- Rural & urban projections from UNDESA or official data
- Labor adjusted using labor force survey trends

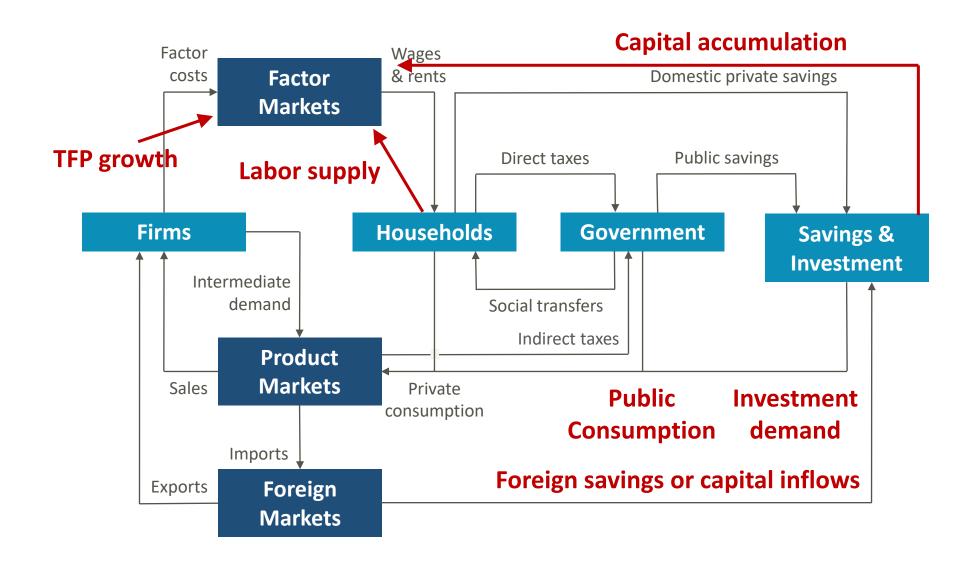
## Land supply & agric. productivity

Based on FAO or official trends (total cultivated area)

## Macroeconomy

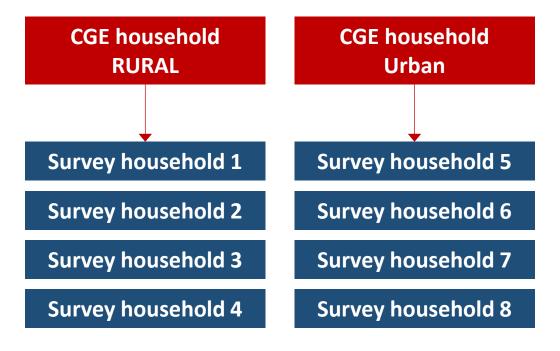
 Baseline assumes trends from previous decade continues (incl. GDP growth by sector, absorption structure, trade balance, remittances/FDI, etc.)

# Recursive Dynamics | Endogenous Capital Accumulation



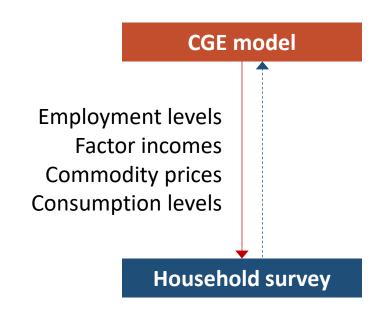
# Microsimulation | Linking to Survey Households

- Each household in the CGE model represents a group of individual households in the household survey (like survey weights)
- Each CGE household is linked to its corresponding survey households



# Microsimulation | Tracking Household Level Outcomes

- Pass down changes in key variables from CGE model to survey
  - Recalculate per capita expenditures for survey households
- Some microsimulation models estimate who loses or gains a job
  - e.g., Occupational choice models
  - Some also pass information back up to the CGE model



# **Additional Accounts**

## Natural resource accounts

Water use by industry and household (for water use rights or user fees)

## Environmental accounts

- Pollution levels for each industry (for pollution taxes or health feedbacks)
- Carbon emissions for each industry and product (for carbon taxes or cap-and-trade schemes)

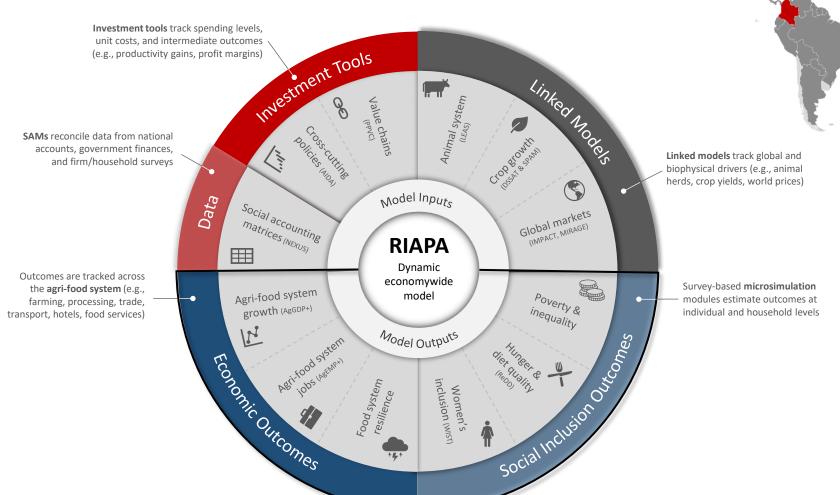
## Financial accounts

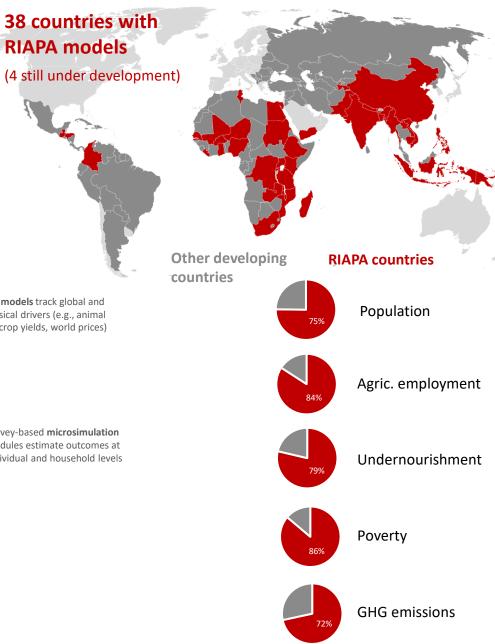
- New institutions (banking sector)
- Assets and liabilities (investments, money holdings, bonds, loans, etc.)
- Allows for CGE models with monetary variables (e.g., money supply, interest rates, inflation, etc.)

# RIAPA | Data & Modeling System

#### Rural Investment and Policy Analysis (RIAPA)

Forward-looking economywide framework that captures entire national economies, unpacks agrifood systems and subnational regions, and tracks how policies, investments, and climate risks affect different sectors, workers and population groups





**RIAPA** models

# **Further Reading**

## Recursive dynamics

 Diao and Thurlow. 2012. A Recursive Dynamic Computable General Equilibrium Model. In Diao et al. (eds.). Strategies and Priorities for African Agriculture: Economywide Perspectives from Country Studies. Washington DC, USA: IFPRI.

#### Microsimulation

- Arndt et al. 2013. Explaining the Evolution of Poverty: The Case of Mozambique. American Journal of Agricultural Economics 95(1): 206-206.
- Pauw and Thurlow. 2011. Agricultural Growth, Poverty, and Nutrition in Tanzania. Food Policy 36(6): 795-804.

#### Environment and natural resources

- Alton et al. 2014. Introducing Carbon Taxes in South Africa. Applied Energy 116(1): 344-354.
- Hassan and Thurlow. 2011. Macro-Micro Feedback Links of Water Management in South Africa: CGE Analyses of Selected Policy Regimes. Agricultural Economics 42(2): 235-247.

### Shocks and extreme events

- Arndt et al. 2008. Higher fuel and food prices: impacts and responses for Mozambique. Agricultural Economics 39: 497-511.
- Pauw et al. 2011. The Economic Costs of Extreme Weather Events: A Hydro-Meteorological CGE Analysis for Malawi. Environment and Development Economics 16(2): 177-198.
- Thurlow et al. 2011. The Impact of the Global Commodity and Financial Crises on Poverty in Vietnam. Journal of Globalization and Development 2(1): 1-29.